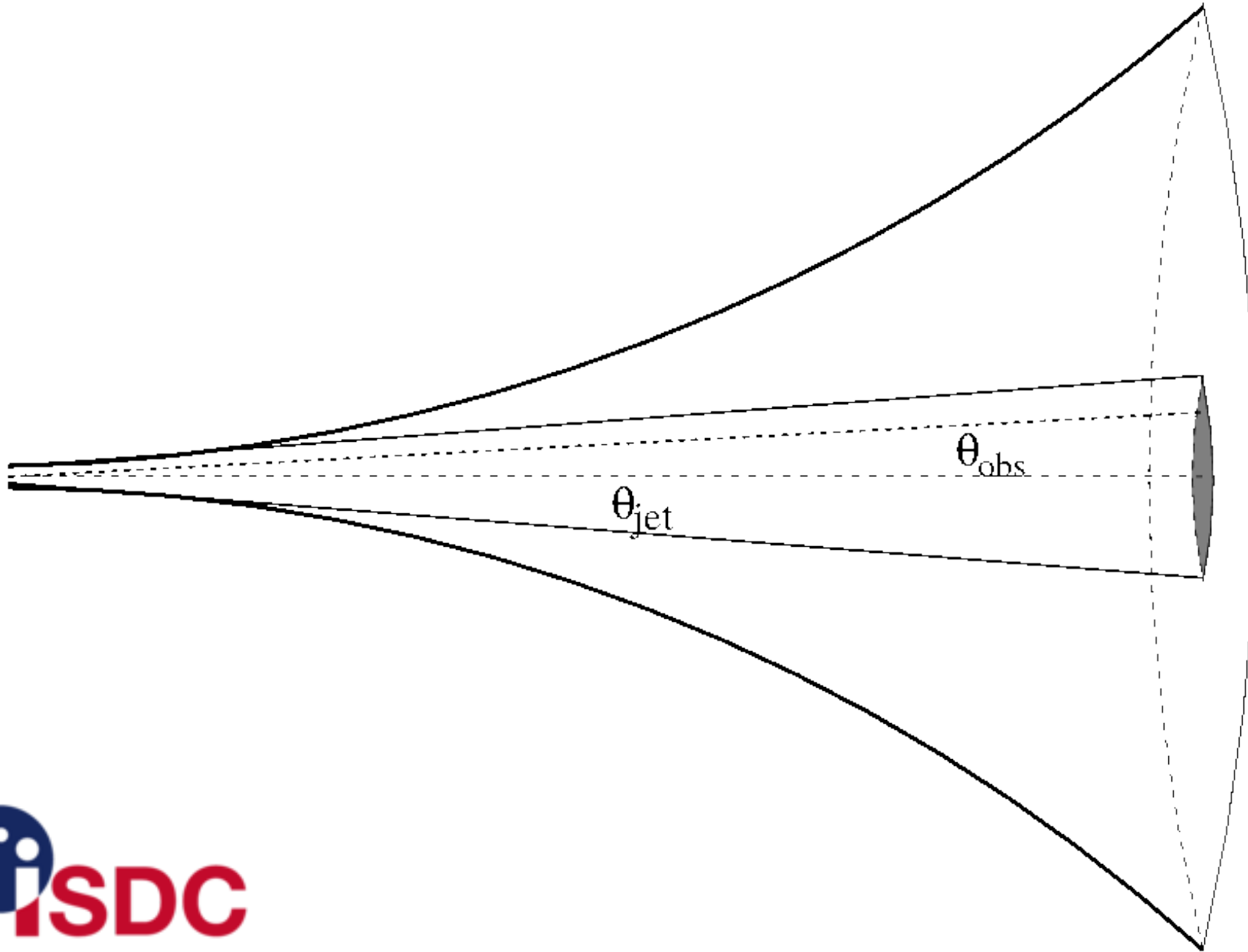
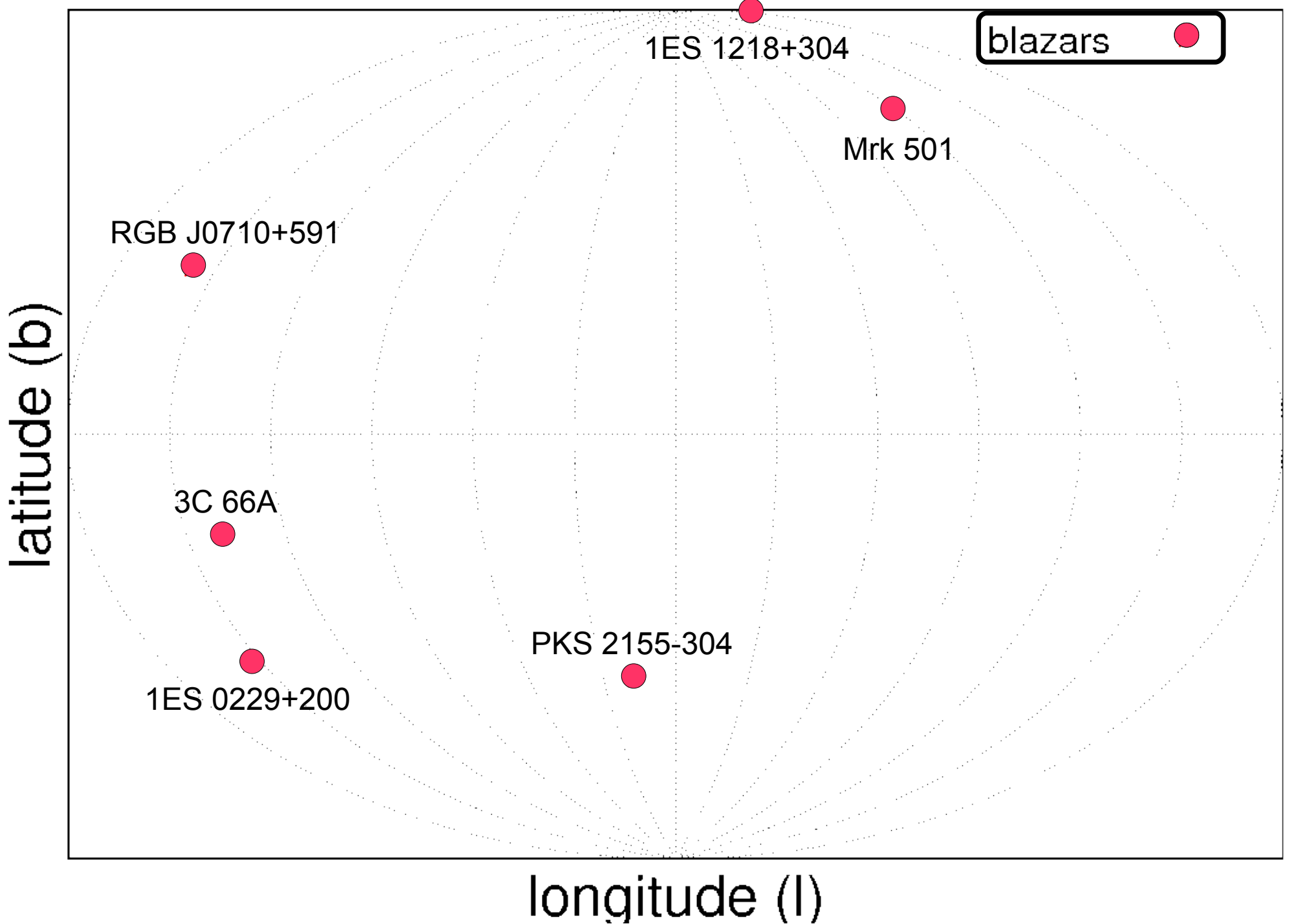


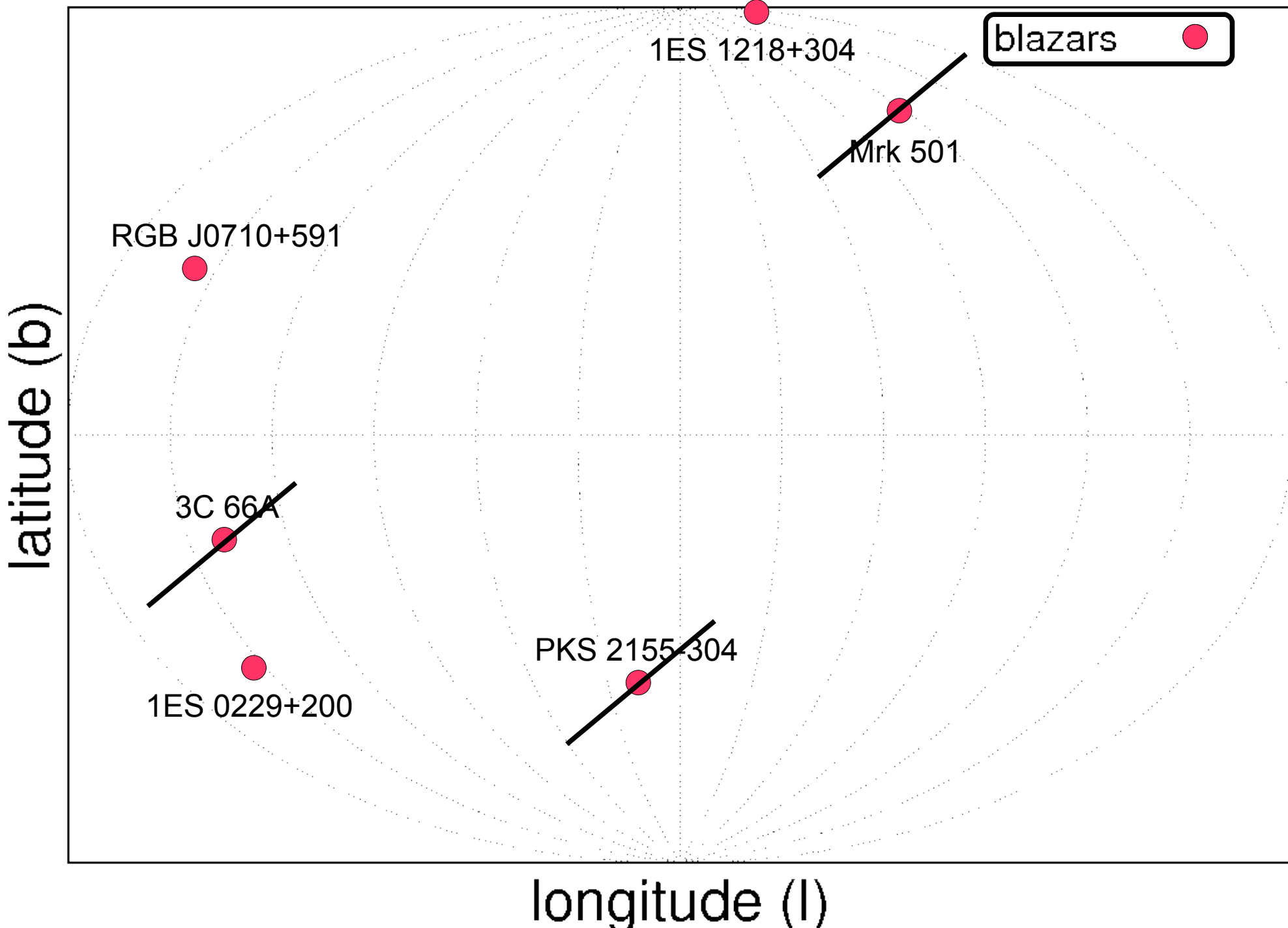
EGMF Constraints from Simultaneous Blazar Observations



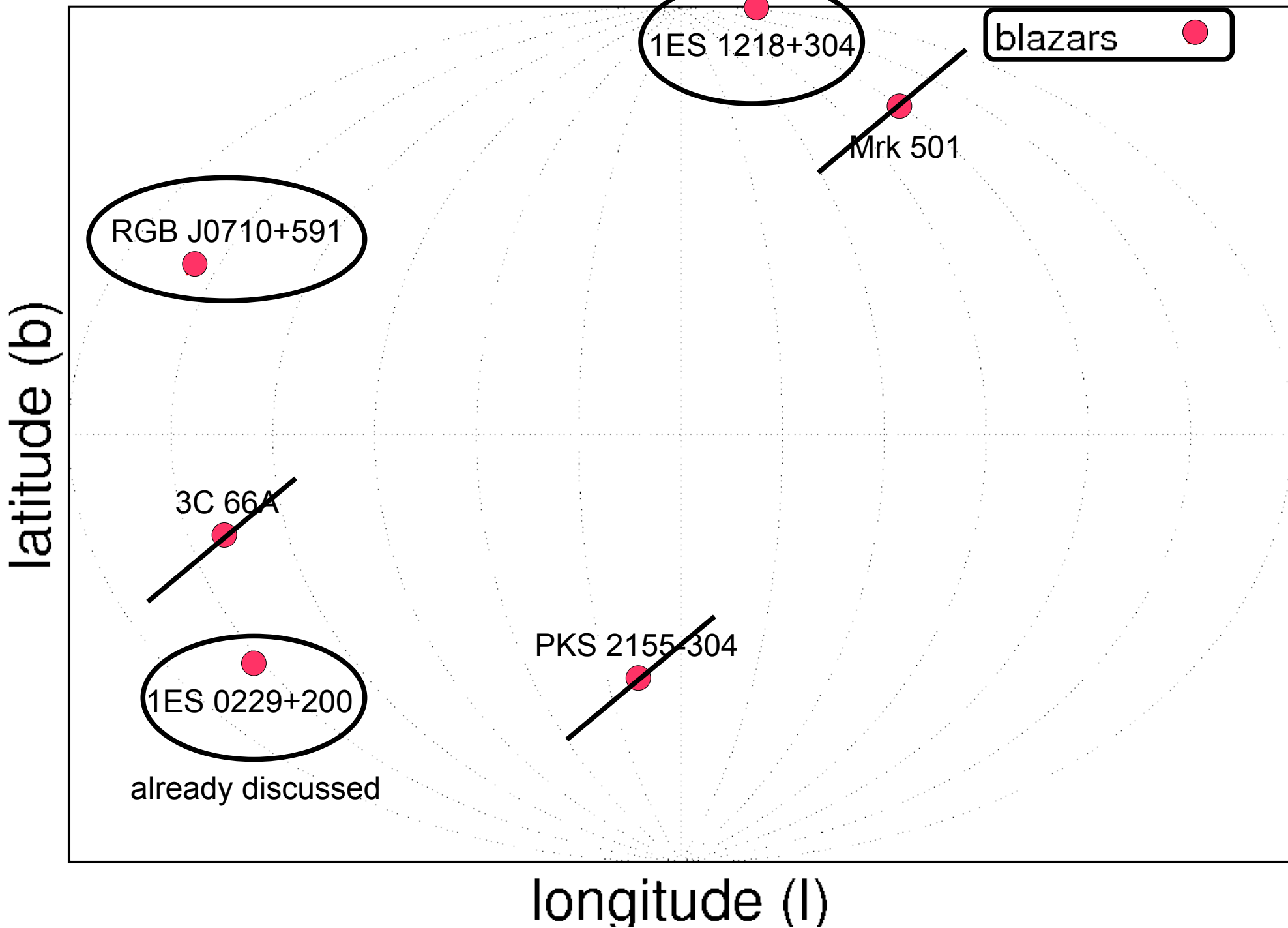
Which Blazars Have Simultaneous Spectra?



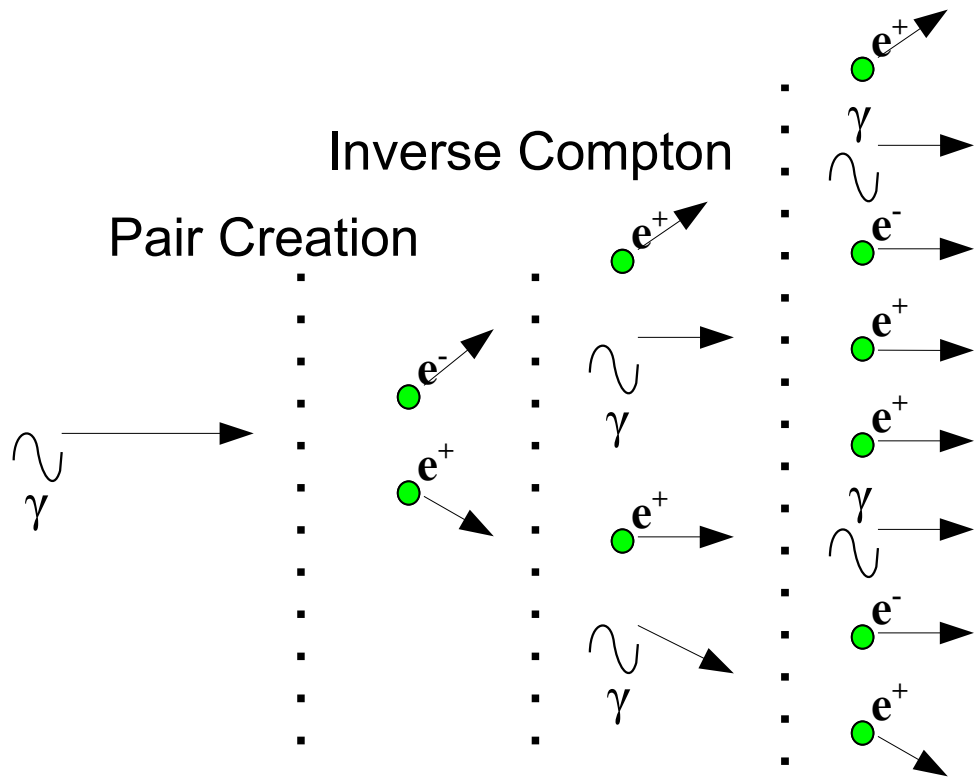
Which of These Have Hard GeV Spectra?



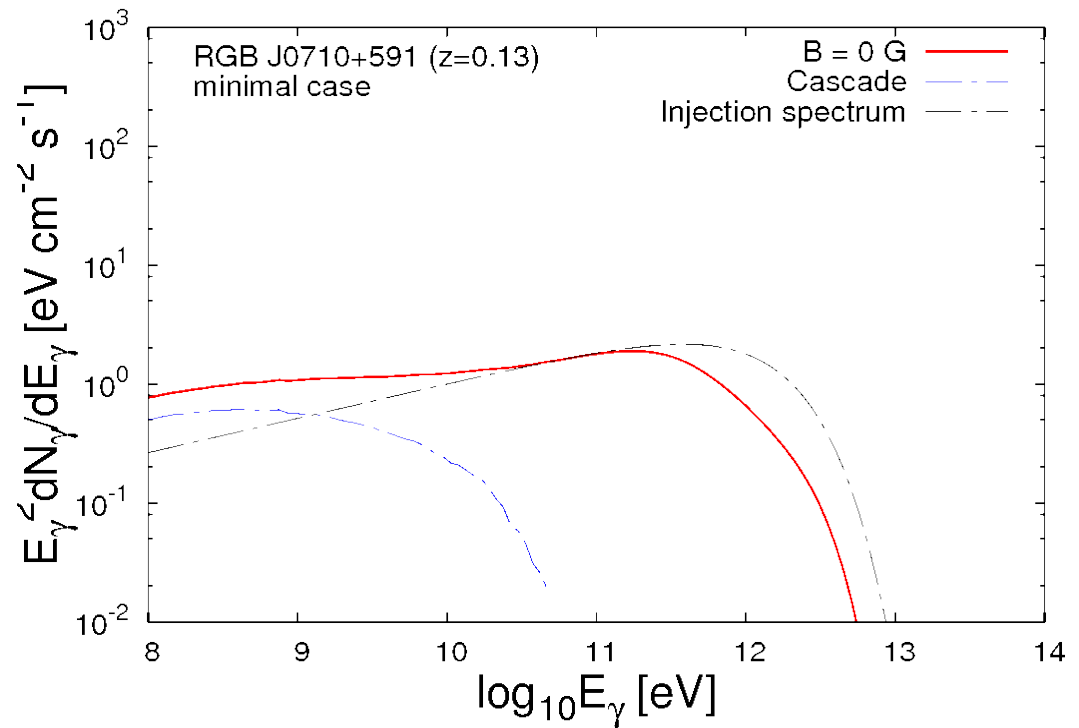
Which of These Have Hard GeV Spectra?



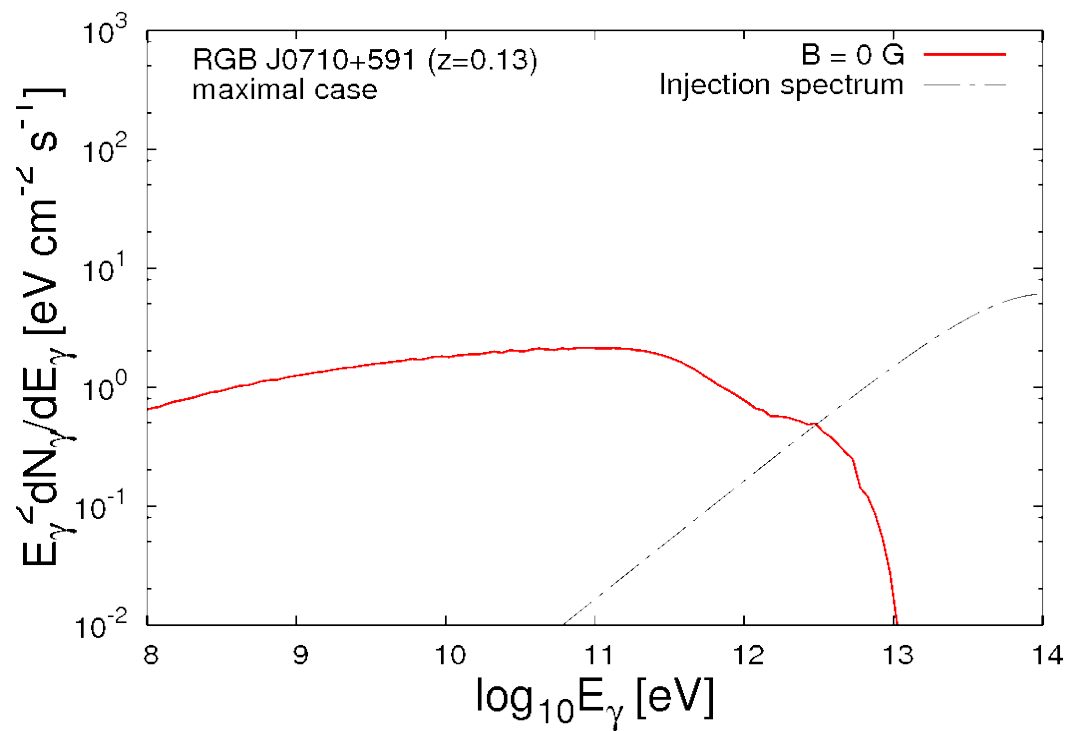
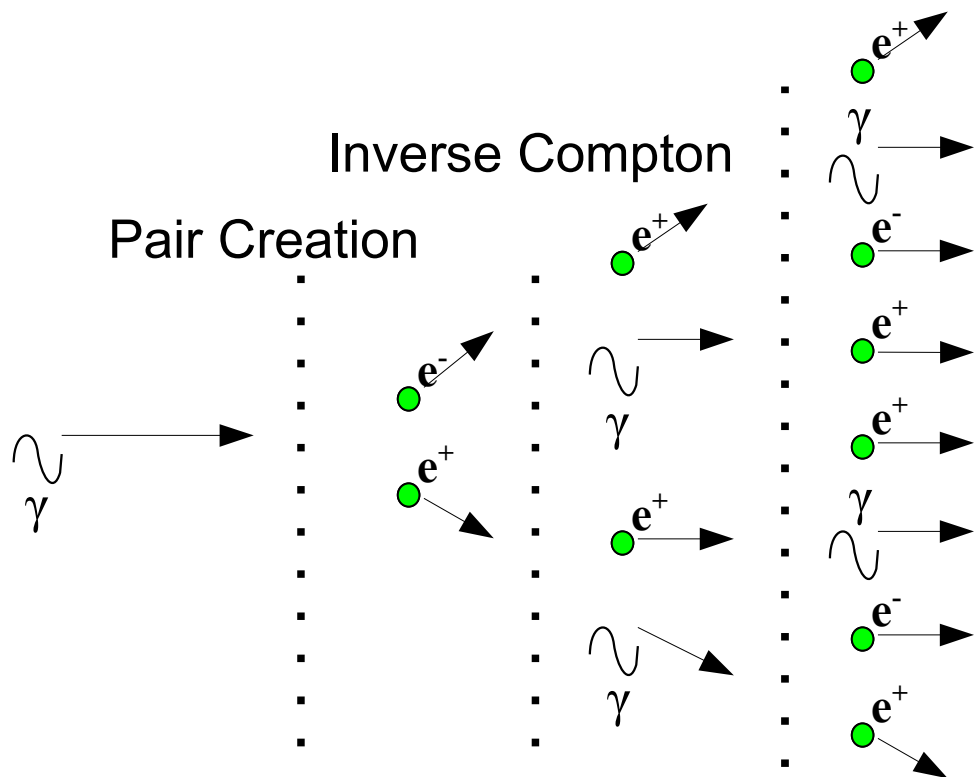
Blazar Fed Cascades (minimal)



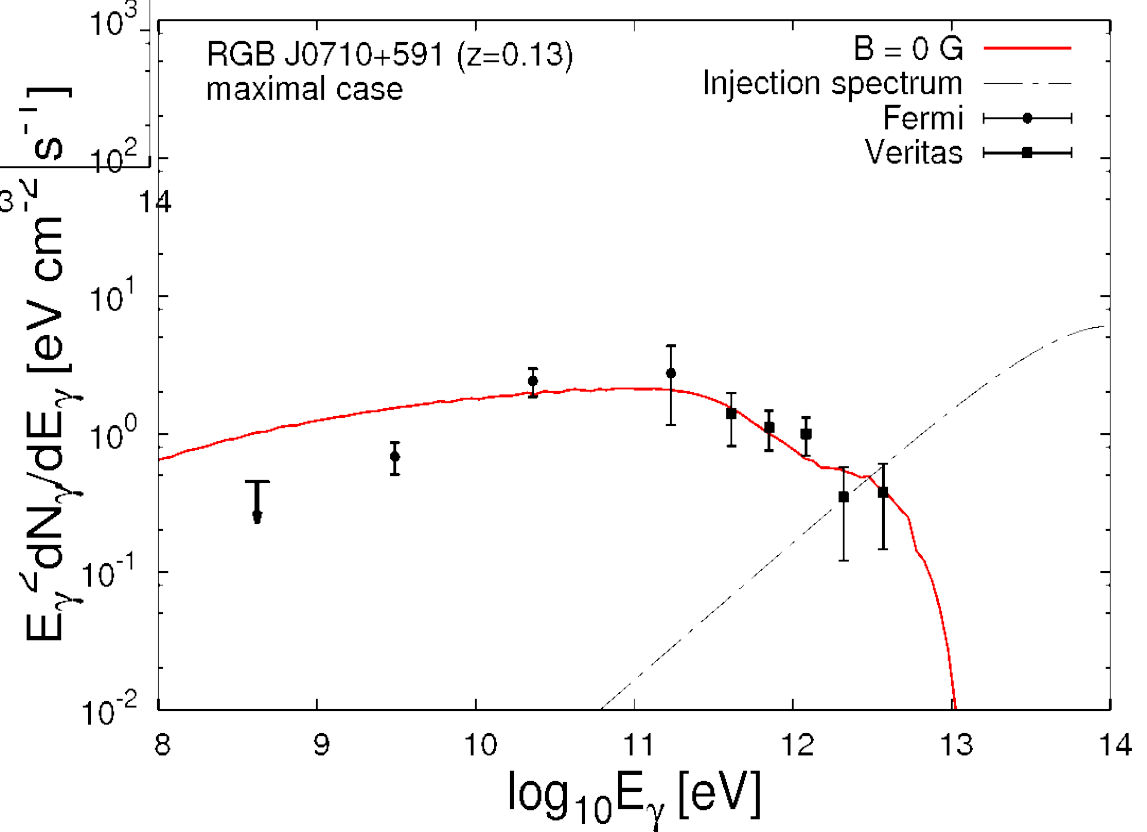
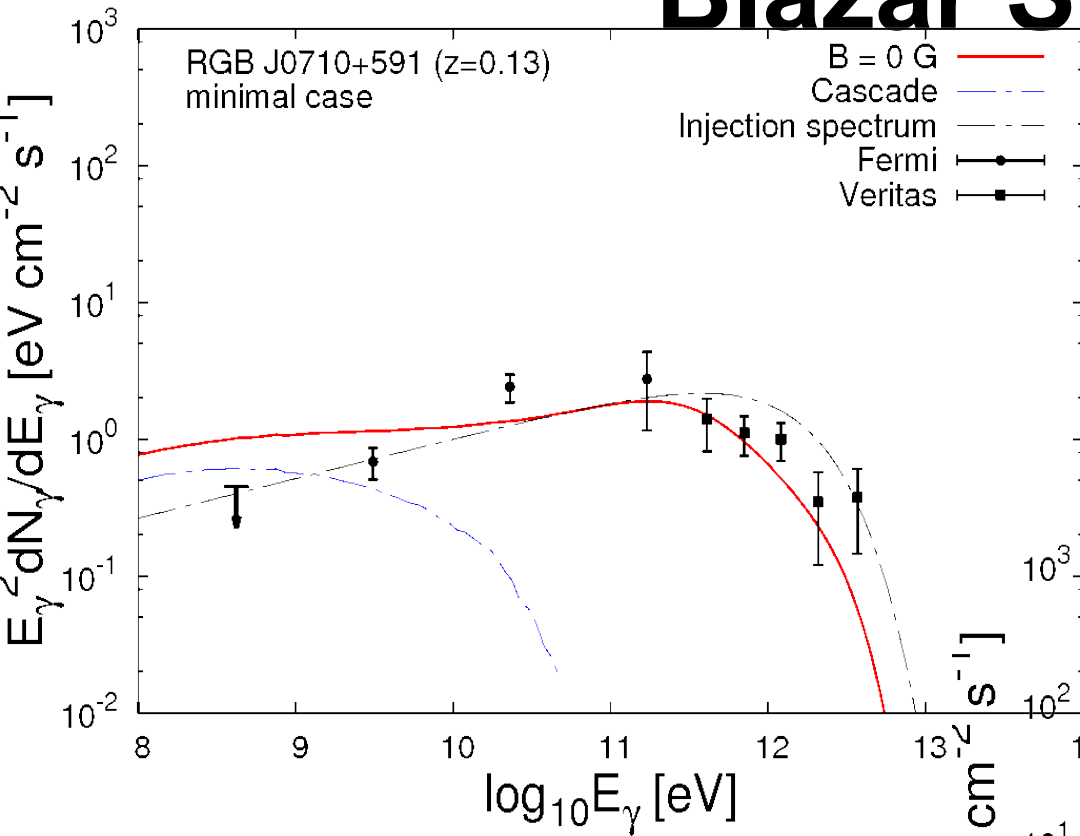
...Few Generations



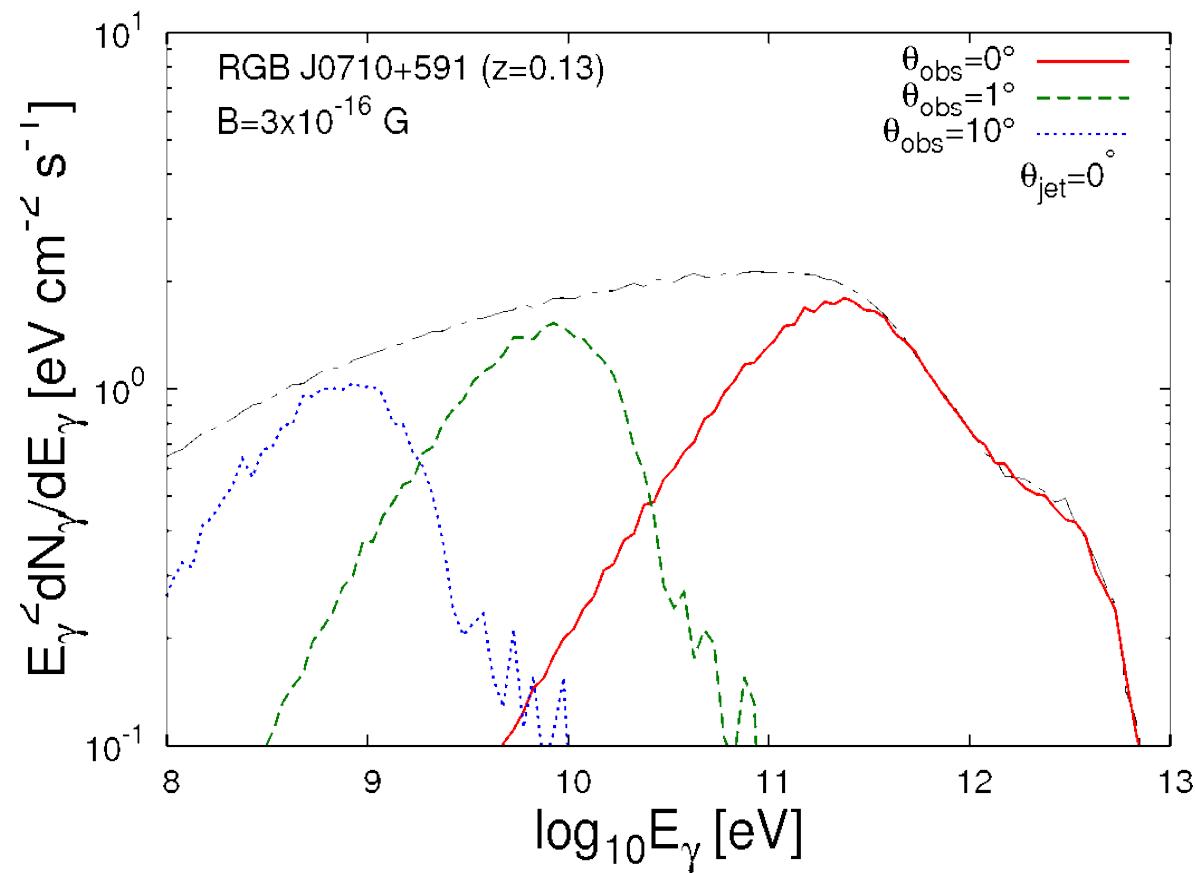
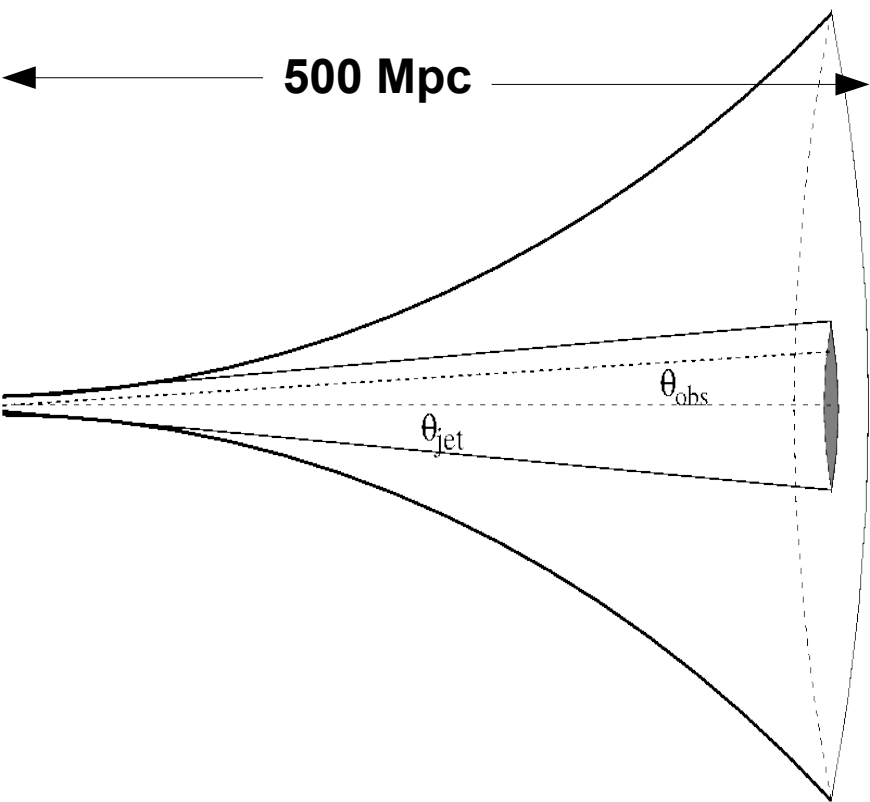
Blazar Fed Cascades (maximal)



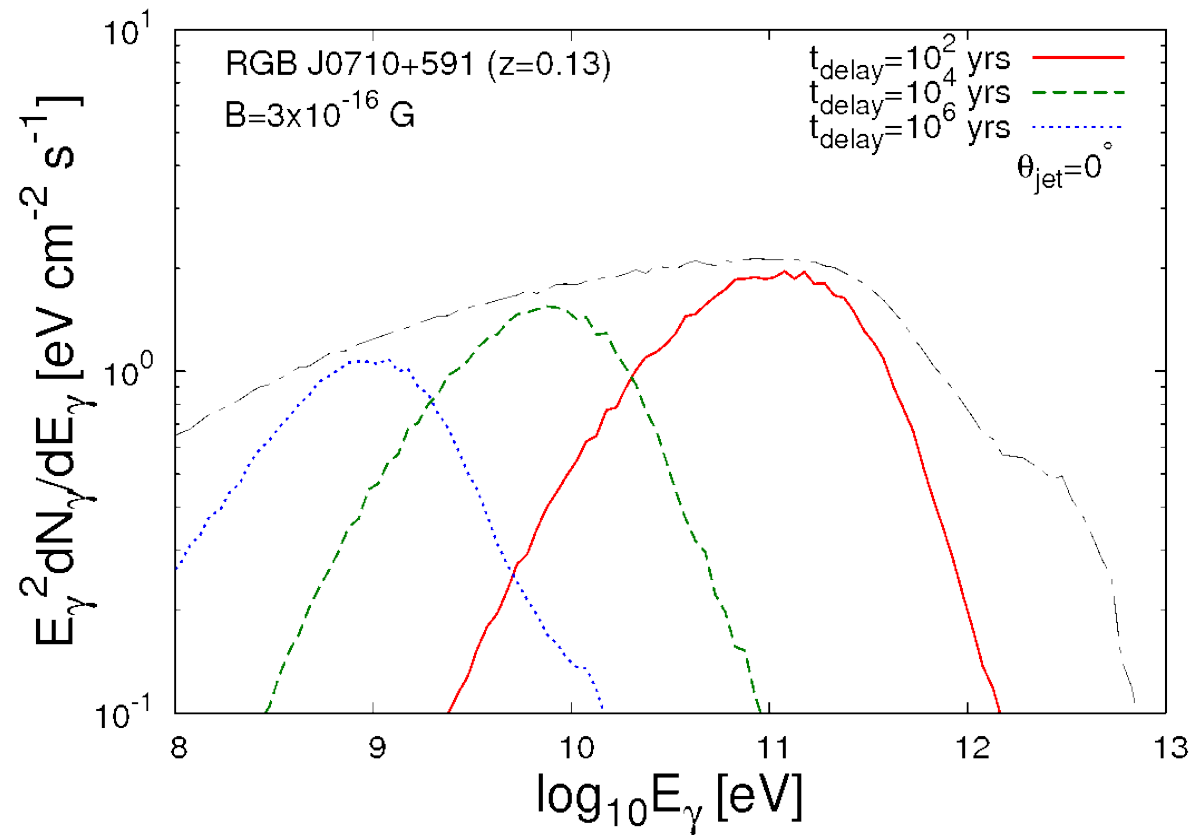
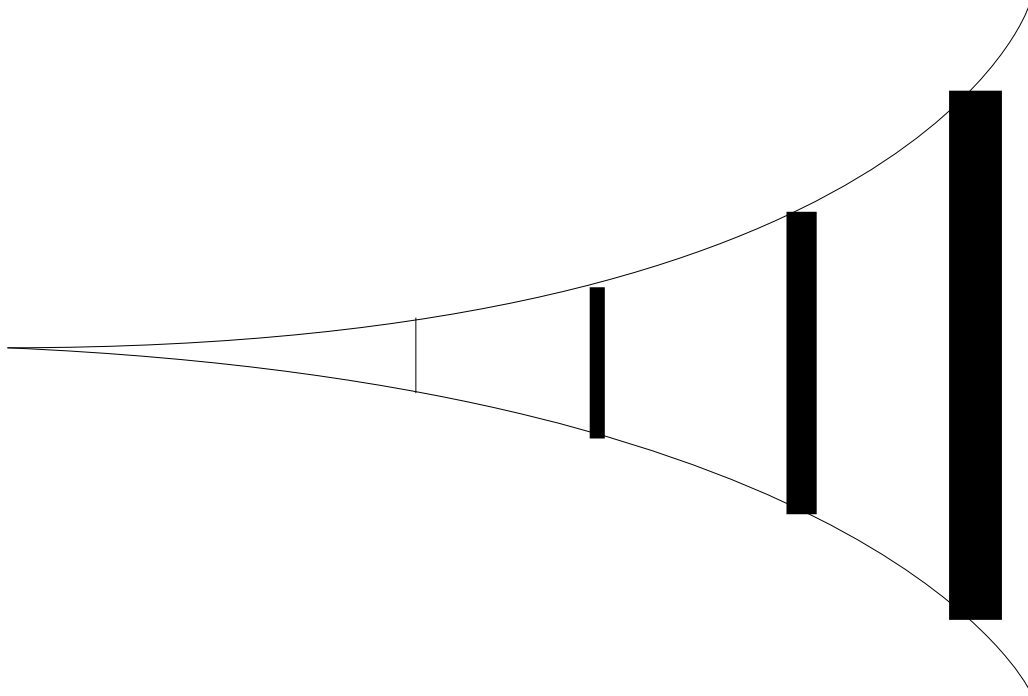
Max + Min Cascade Contributions to Blazar Spectra?



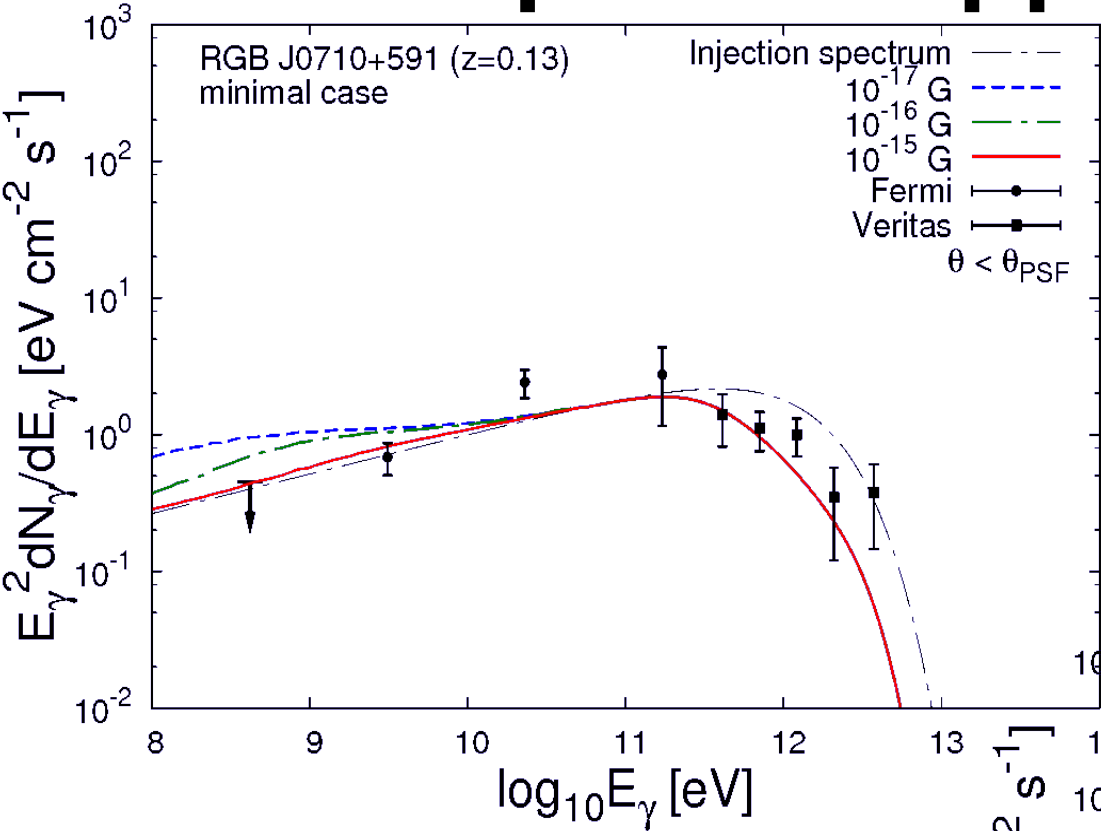
Spatial Decomposition of Spectrum



Temporal Decomposition of Spectrum

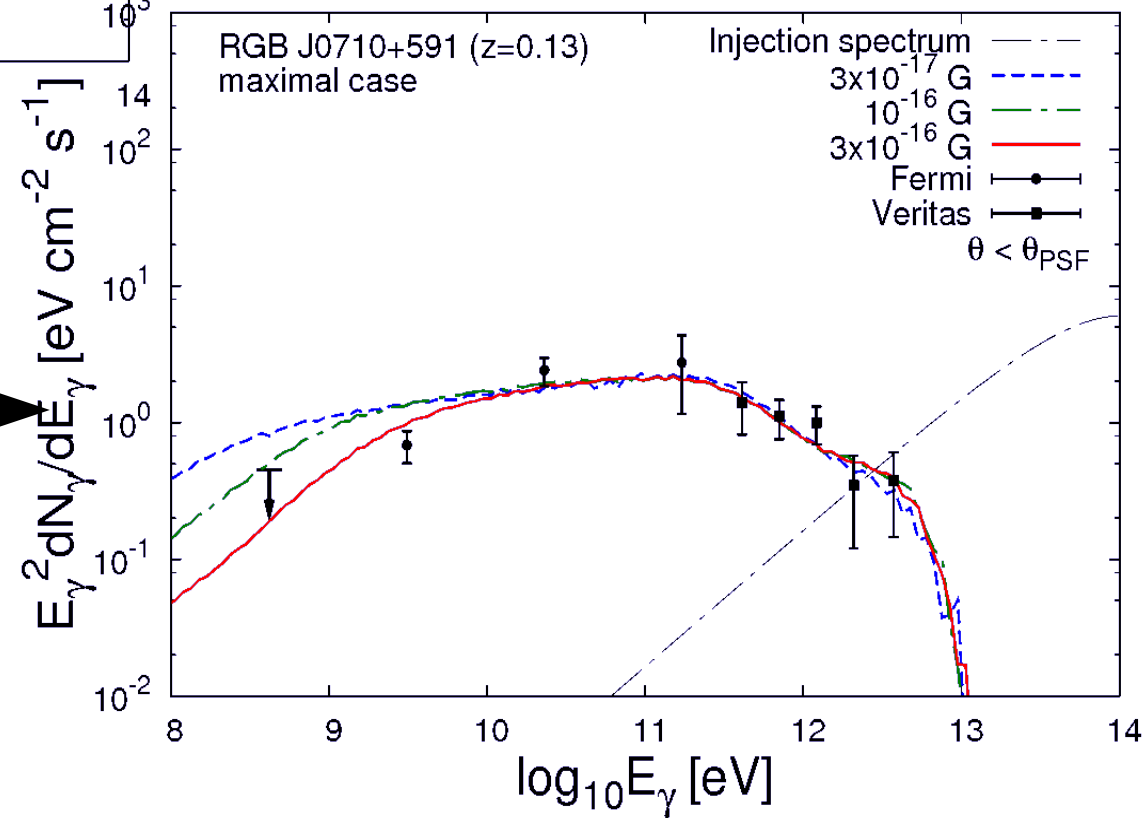


B-Field Spatial Suppression of Cascade

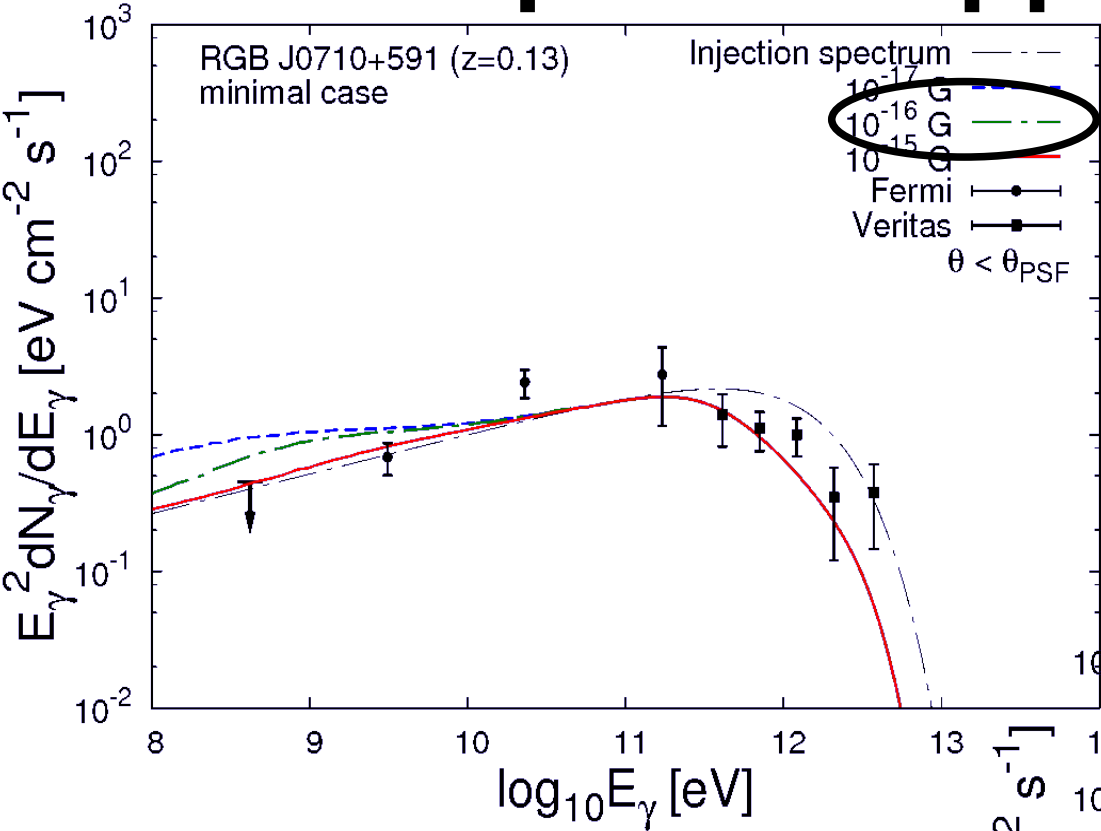


Minimal case

Maximal case

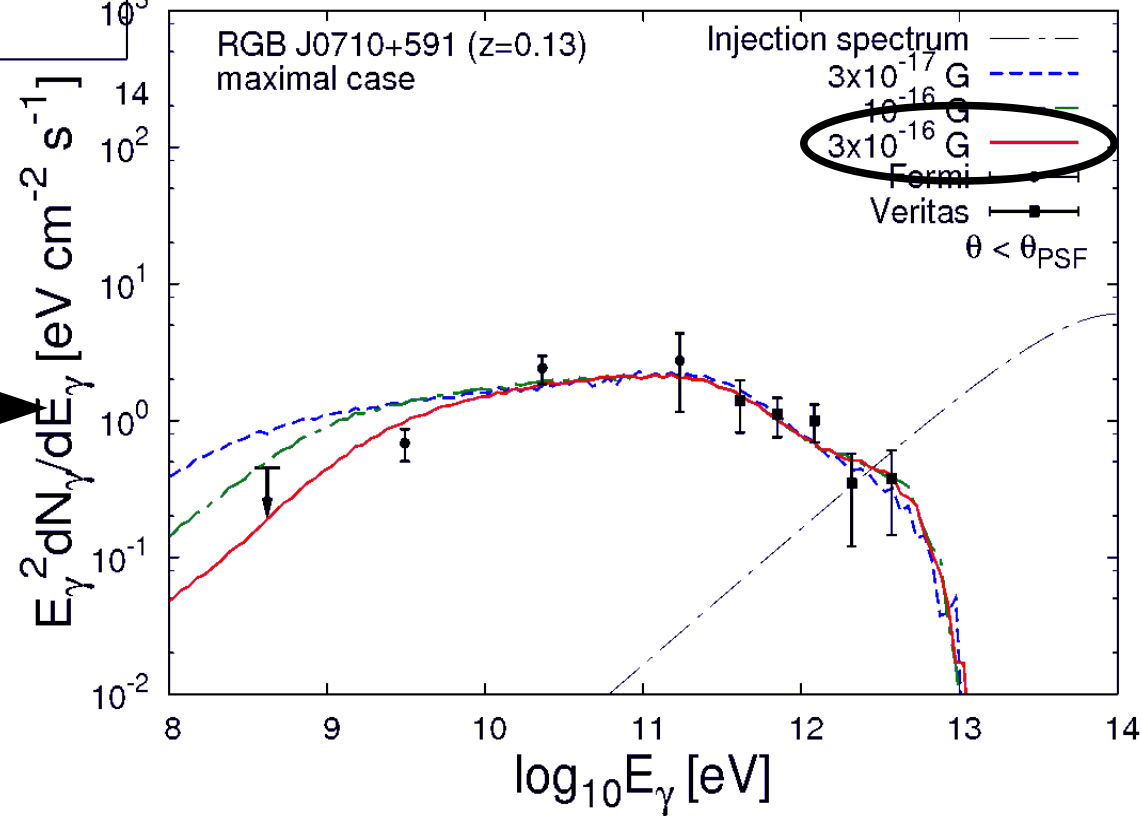


B-Field Spatial Suppression of Cascade

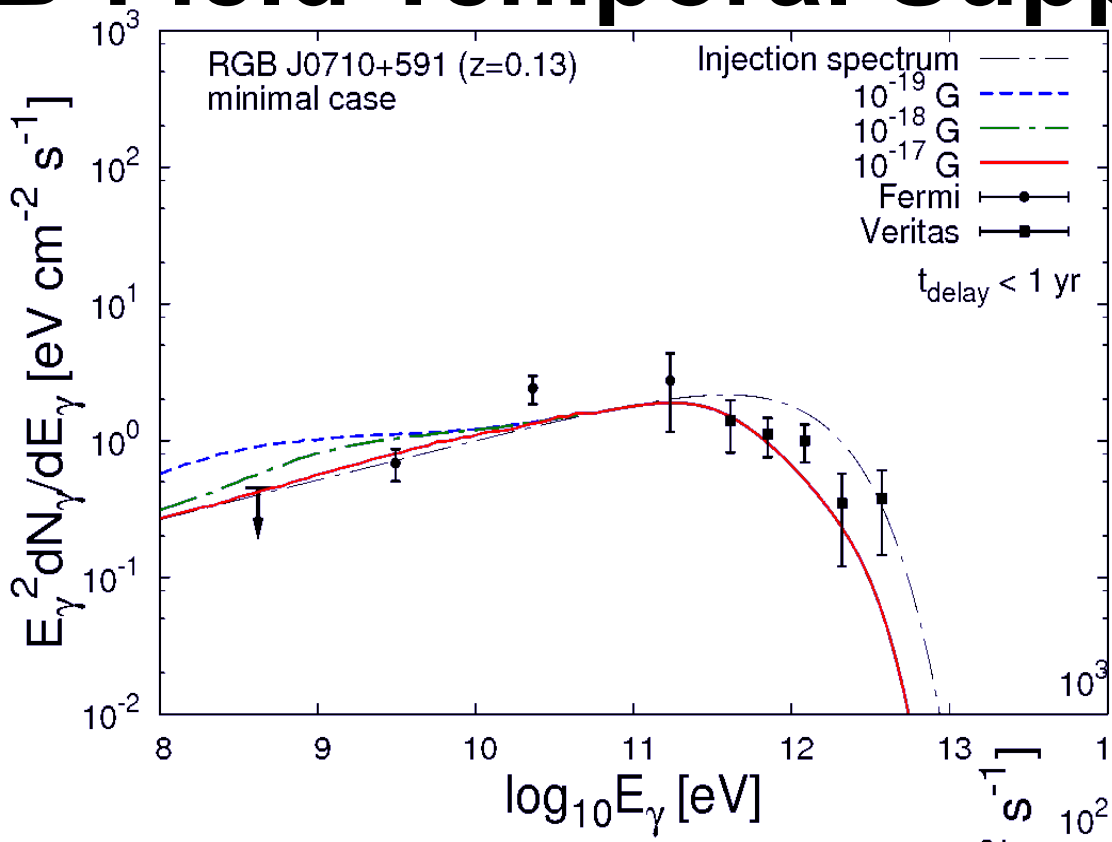


**Minimal
case**

**Maximal
case**

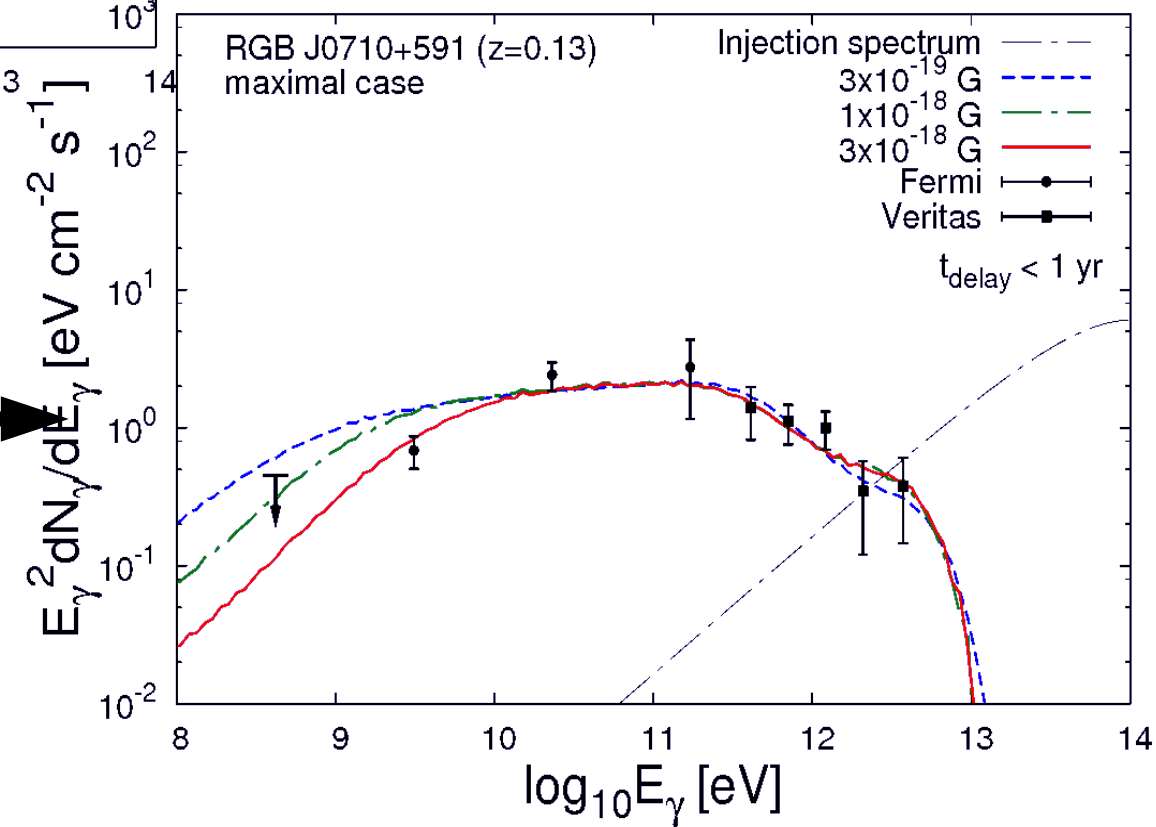


B-Field Temporal Suppression of Cascade

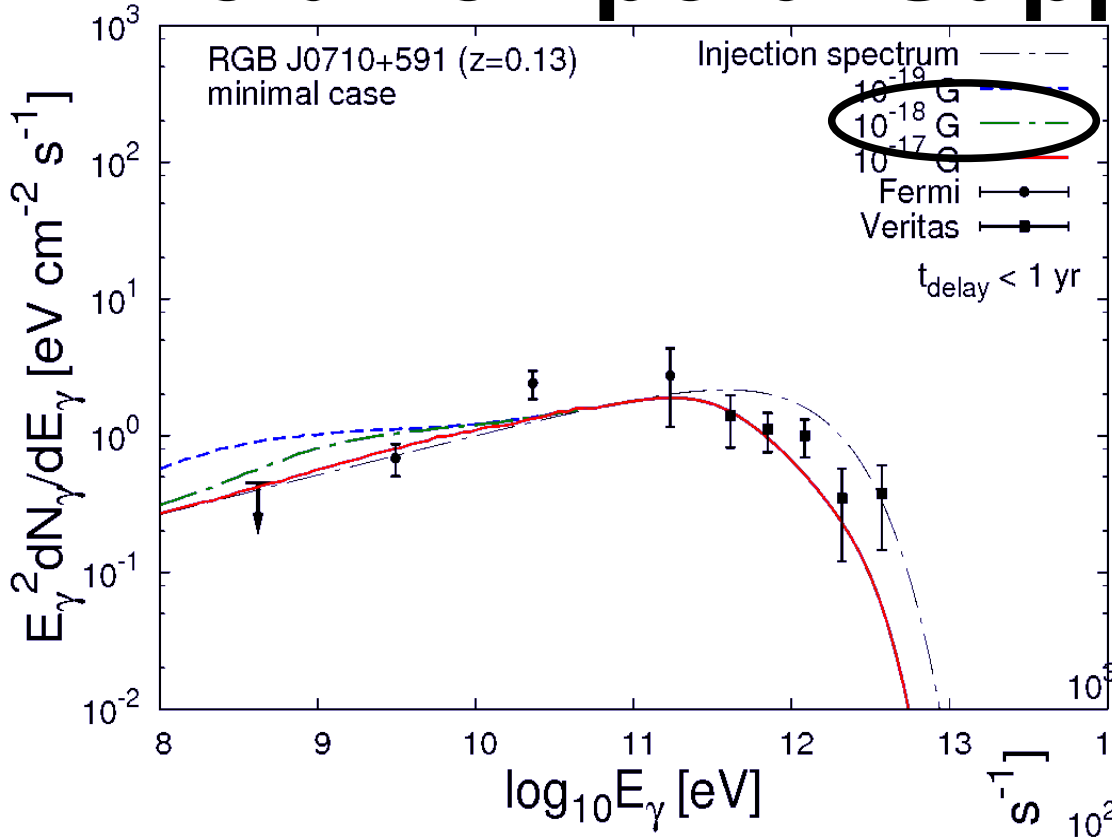


Minimal case

Maximal case



B-Field Temporal Suppression of Cascade

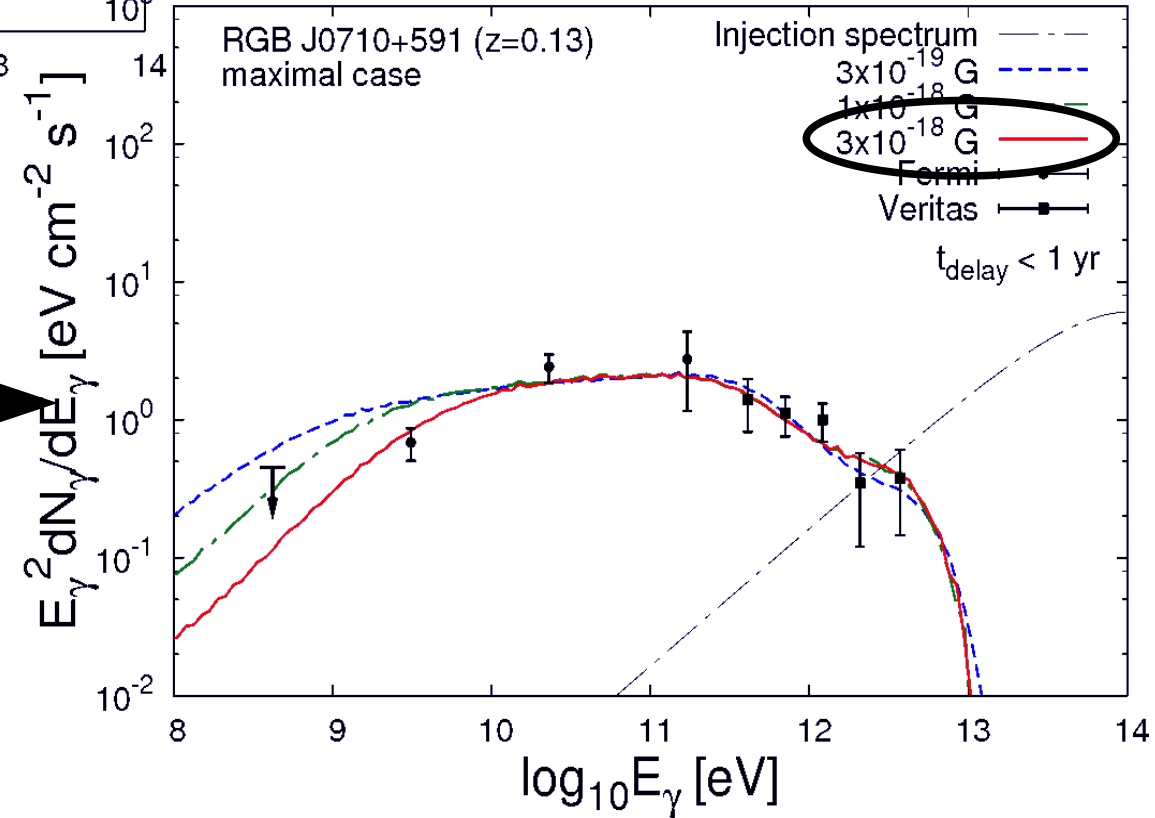


Minimal case

←

Maximal case

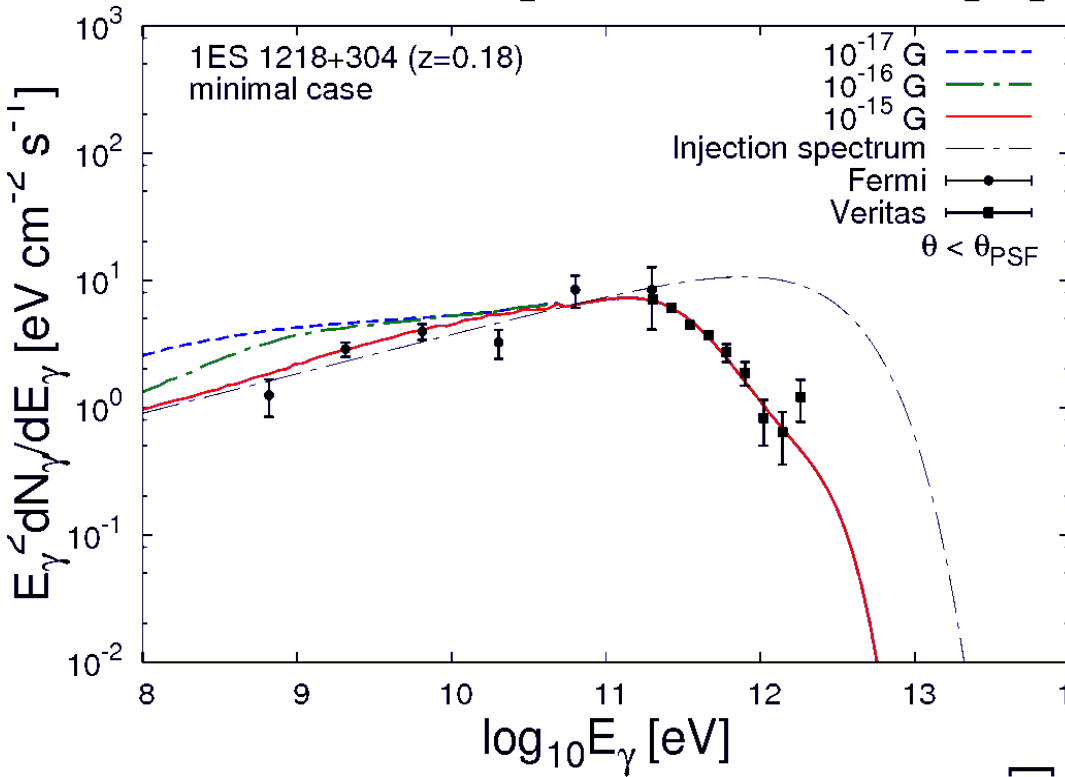
→



Conclusions

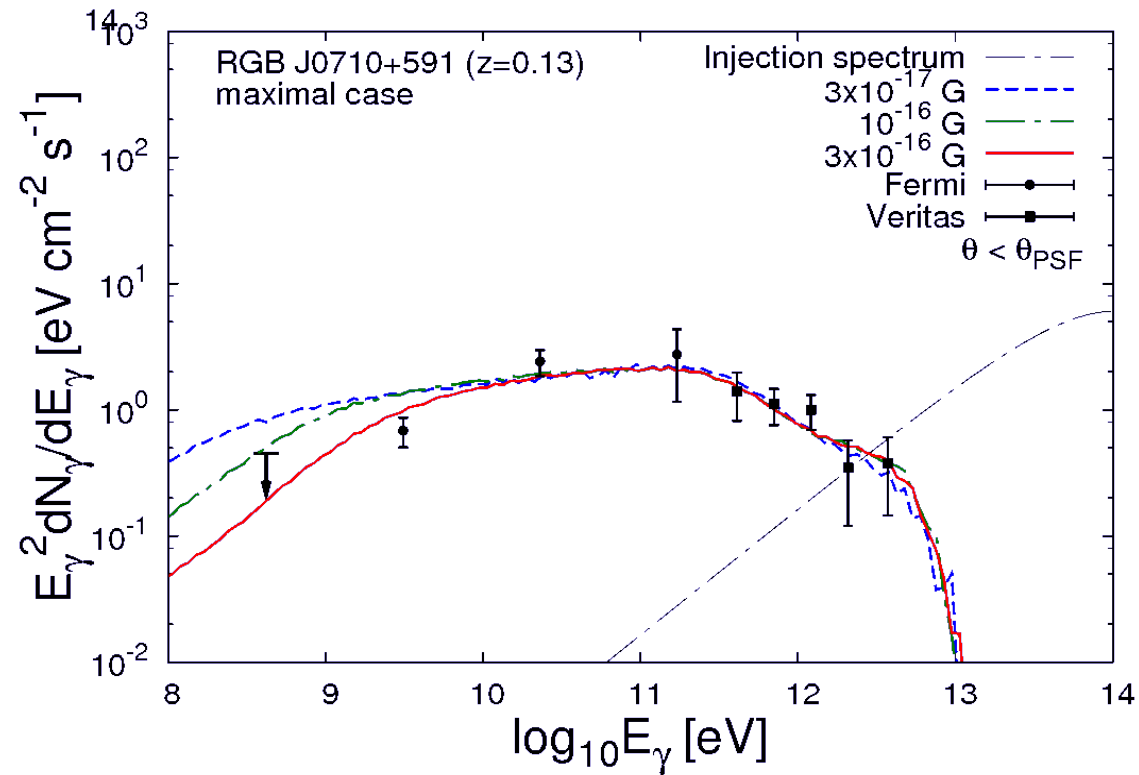
- Simultaneous GeV and TeV observations of 3 blazars with hard (GeV) spectra suggest a suppression of the cascade component is required
- Both spatial and temporal suppression mechanisms of the cascade component are viable
- A spatial suppression origin leads to a lower bound of $B \sim 10^{-16} \text{G}$ (this bound quietly assumes that the blazar is not variable on $\sim 10^5$ yr timescales).
- A temporal suppression origin, with variability on ~ 1 yr timescales leads to a much more conservative lower bound of $B \sim 10^{-18} \text{G}$

B-Field Spatial Suppression of Cascade

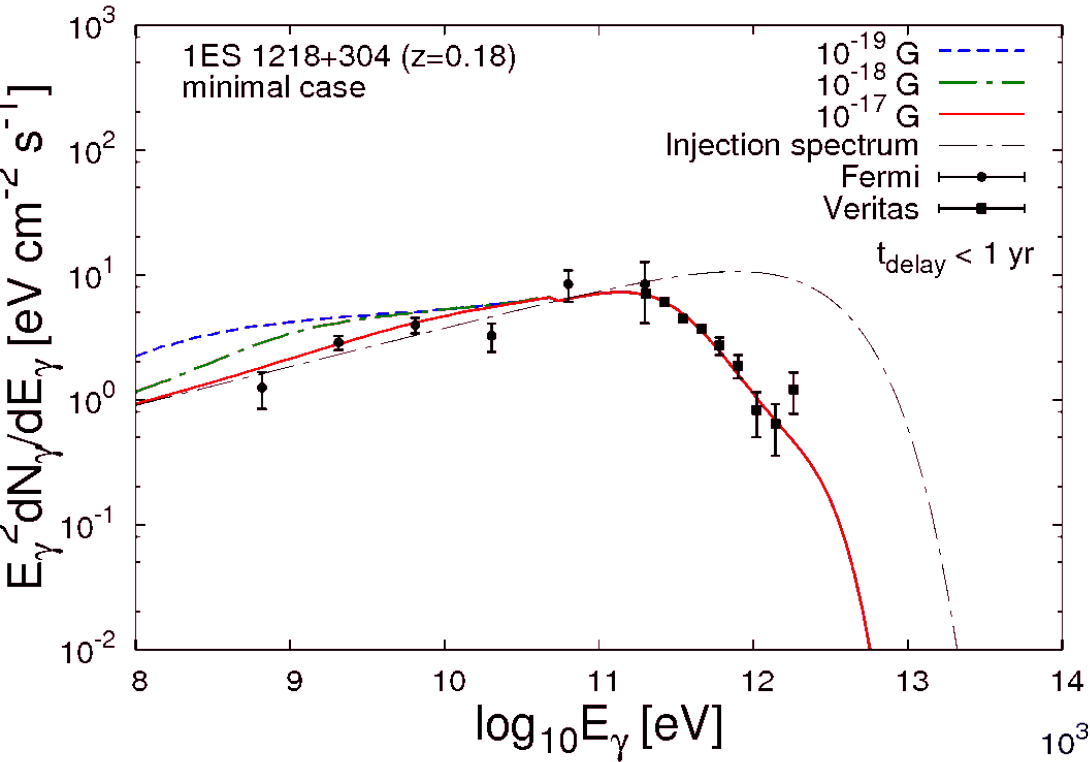


Minimal
case

Maximal
case

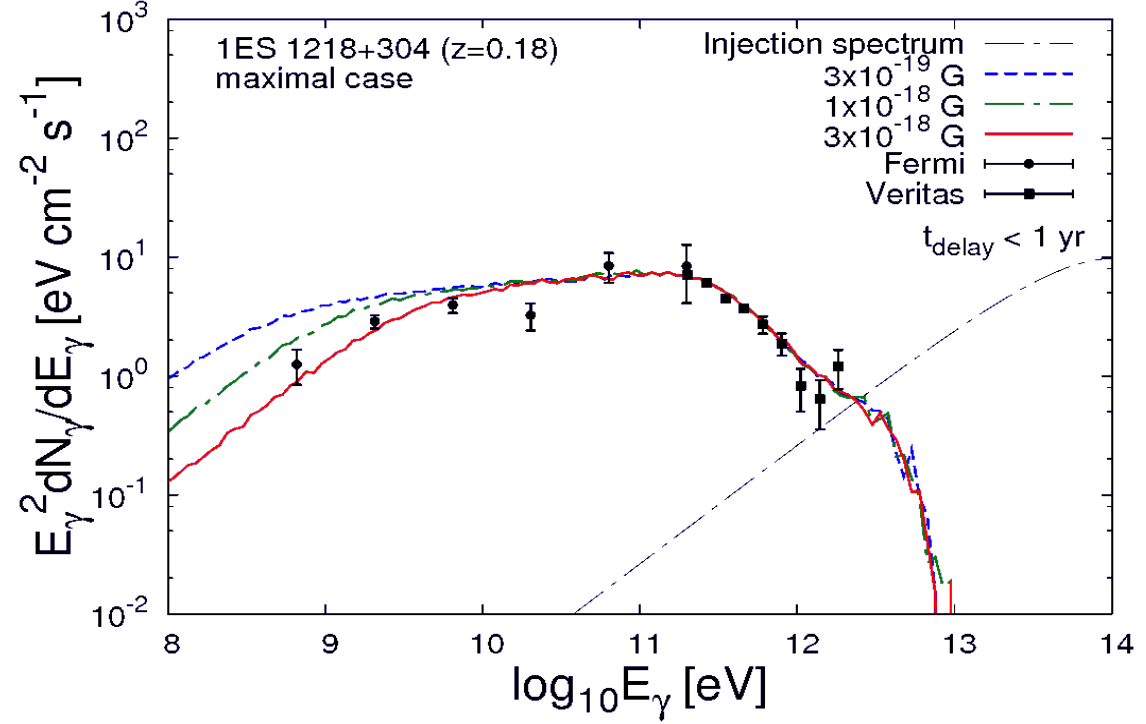


B-Field Temporal Suppression of Cascade

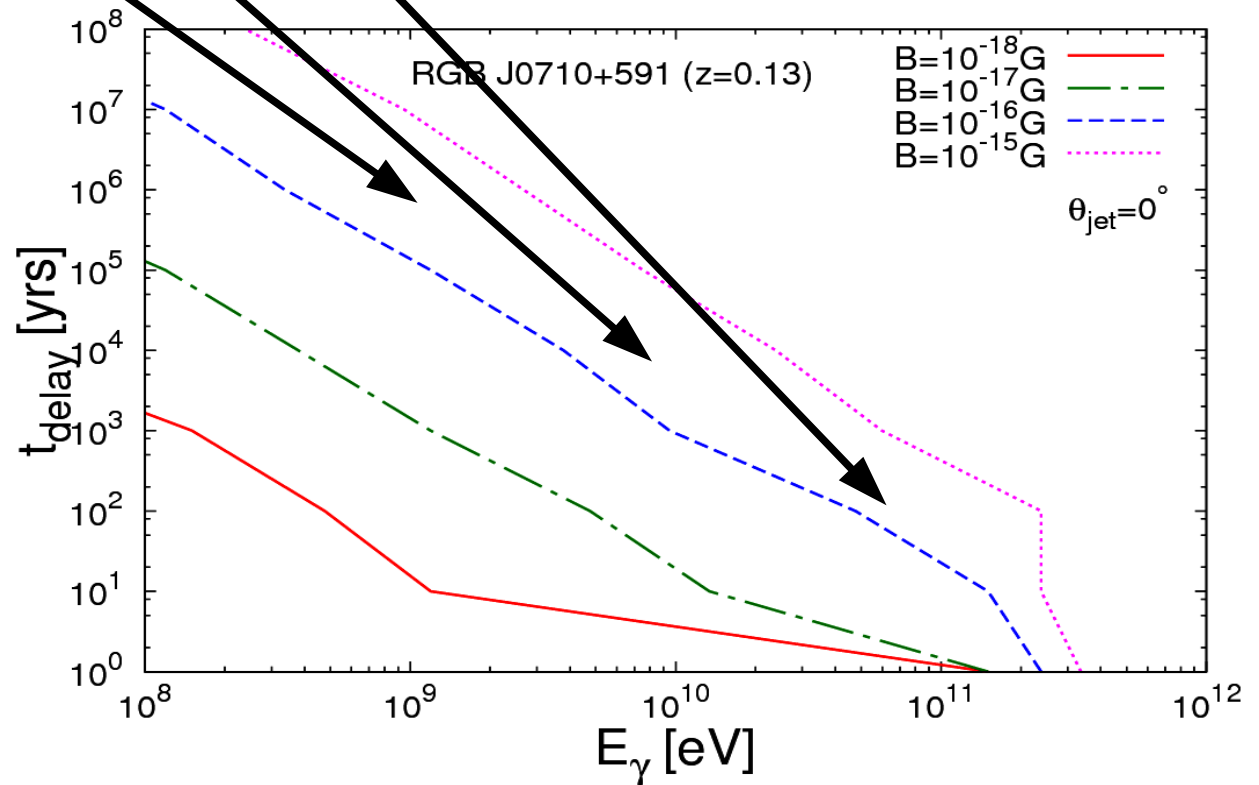
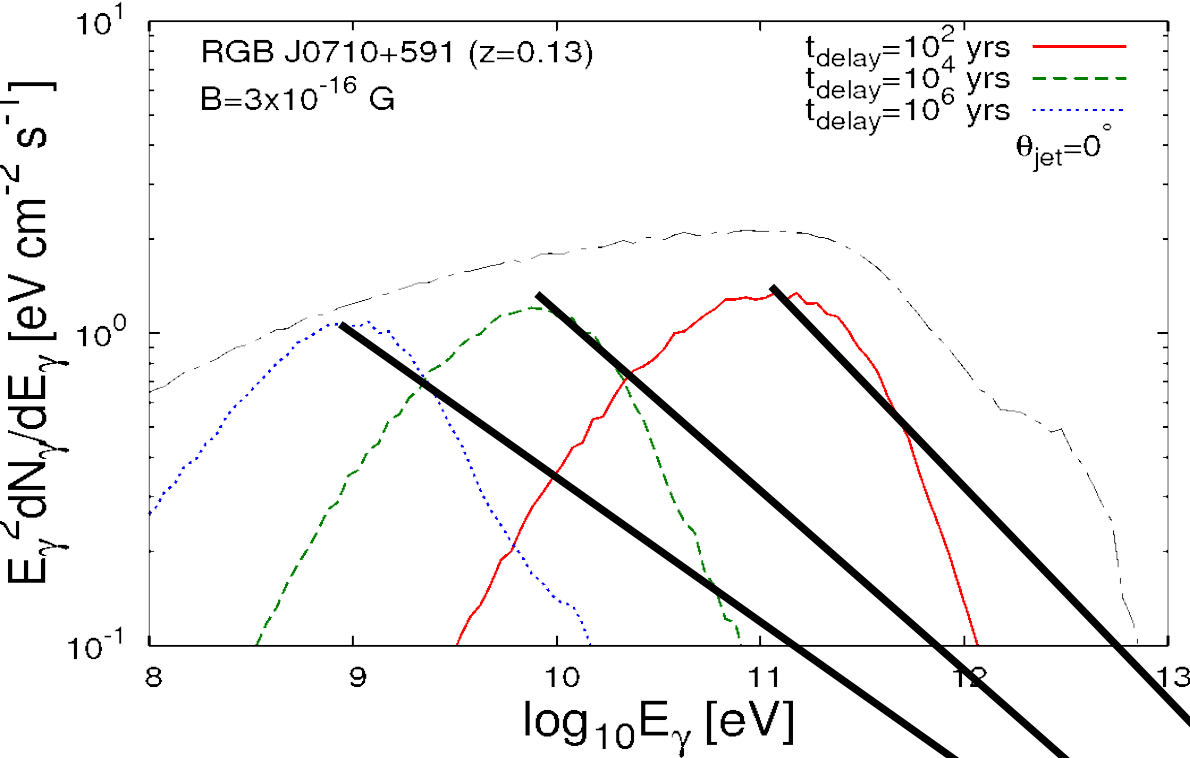


Minimal case

Maximal case



Temporal Decomposition of Spectrum



Why 10^{-15} G?

Need to suppress IC flux with an energy of $\sim 10^9$ eV

$$E_{\gamma}^{\text{IC}} \approx \Gamma_e^2 E_{\gamma}^{\text{bg}}$$

$$E_{\gamma}^{\text{IC}} = 10^9 \text{ eV} \quad E_{\gamma}^{\text{bg}} \approx 10^{-3} \text{ eV}$$

$$\text{So, } \Gamma_e = 10^6 \quad \text{ie. } E_e \approx \text{TeV}$$

Why 10^{-15} G?

So, $\Gamma_e = 10^6$ ie. $E_e \approx \text{TeV}$

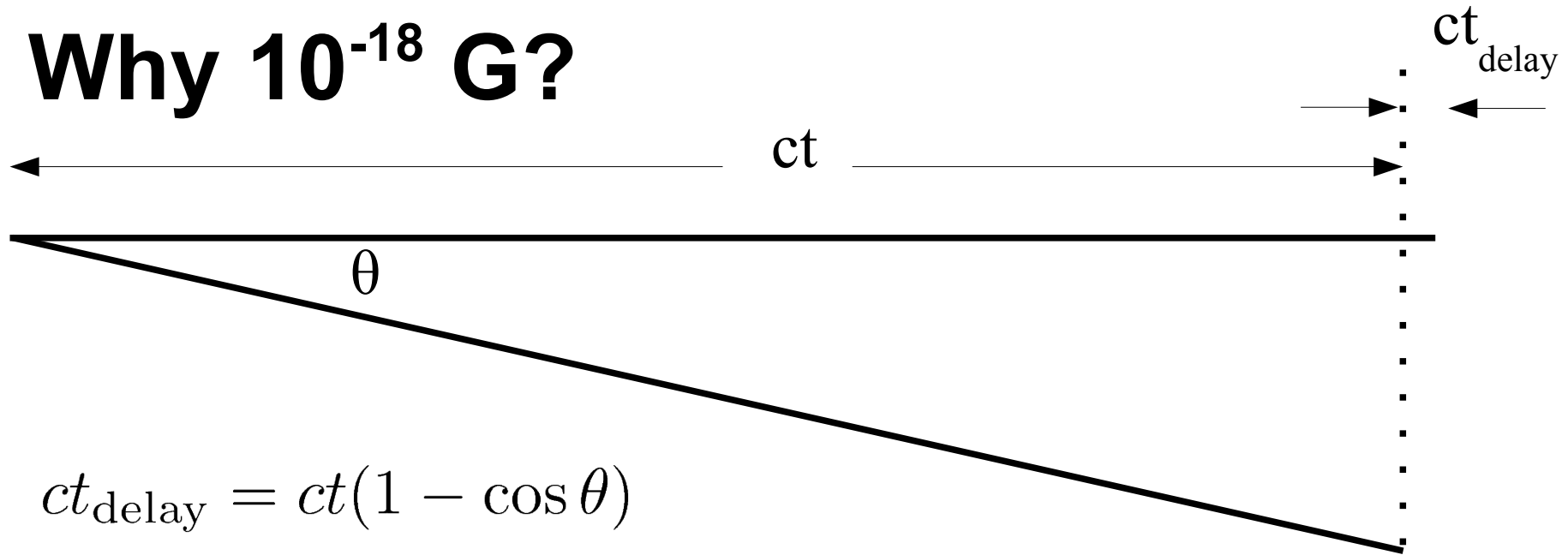
IC flux suppression occurs when electron flux starts to be isotropised.

The deflection angle in each mag. patch is

$$\alpha = \frac{L_{\text{coh}}}{R_{\text{Larmor}}}$$

$$R_{\text{Larmor}} \approx 1 \left(\frac{E_e}{\text{TeV}} \right) \left(\frac{10^{-15} \text{ G}}{B} \right) \text{ Mpc}$$

Why 10^{-18} G?



$$ct_{\text{delay}} = ct(1 - \cos \theta)$$

$$ct_{\text{delay}} \approx \theta^2 ct$$

$$\theta = \alpha \left(\frac{ct}{L_{\text{coh}}} \right)^{1/2} = \frac{L_{\text{coh}}}{R_{\text{Larmor}}} \left(\frac{ct}{L_{\text{coh}}} \right)^{1/2}$$

$$R_{\text{Larmor}} \approx 1 \left(\frac{E_e}{\text{TeV}} \right) \left(\frac{10^{-18} \text{ G}}{B} \right) \text{ Gpc}$$

Why 10^{-18} G?

$$ct_{\text{delay}} \approx \theta^2 ct$$

$$\theta = \alpha \left(\frac{ct}{L_{\text{coh}}} \right)^{1/2} = \frac{L_{\text{coh}}}{R_{\text{Larmor}}} \left(\frac{ct}{L_{\text{coh}}} \right)^{1/2}$$

$$R_{\text{Larmor}} \approx 1 \left(\frac{E_e}{\text{TeV}} \right) \left(\frac{10^{-18} \text{ G}}{B} \right) \text{ Gpc}$$

Since, $ct = 500 \text{ Mpc}$

$$t_{\text{delay}} = 10^3 \left(\frac{10^{-18} \text{ G}}{B} \right)^2 \text{ yr}$$