

ANISOTROPIC CR DIFFUSION IN THE GALAXY

Gwenael Giacinti (MPIK Heidelberg)

with Ruben Lopez-Coto, Michael Kachelriess,
Dmitri V. Semikoz

GG, Kachelriess & Semikoz, JCAP 07, 051 (2018) [arXiv:1710.08205]

Lopez-Coto & GG, MNRAS 479, 4526 (2018) [arXiv:1712.04373]

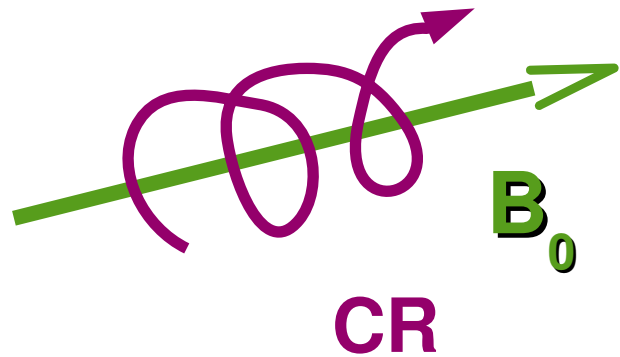


OUTLINE :

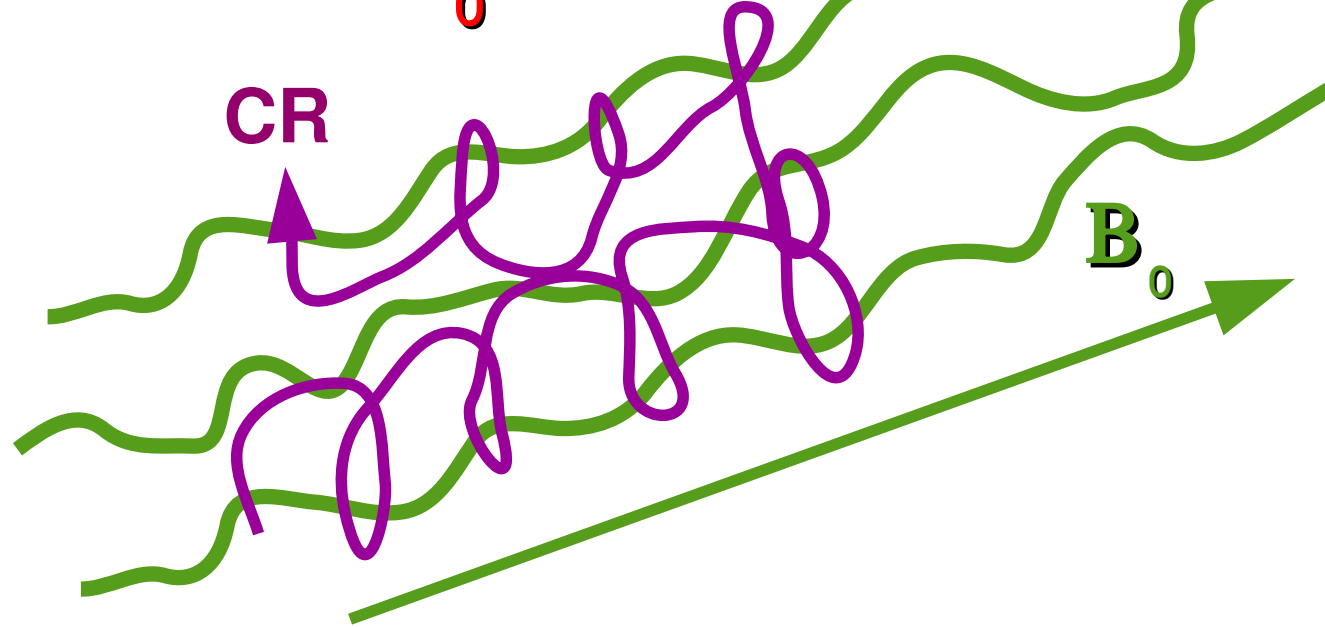
- I – γ -ray emission around Geminga as a probe of the surrounding turbulence**
- II – Anisotropic CR diffusion in the Milky Way and Galactic magnetic field models**

Perpendicular/Parallel diffusion coeffs.

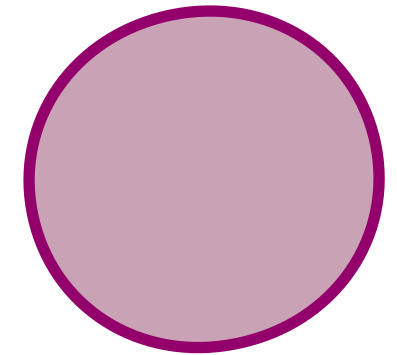
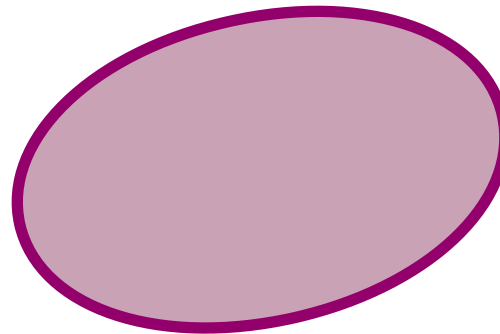
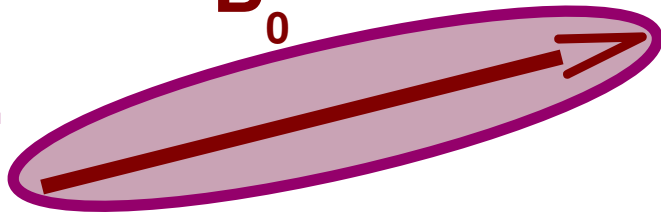
$\delta B = 0$



$\delta B/B_0 \ll 1$



B_0



$\delta B/B_0 \ll 1$

Increasing turbulence

$\delta B/B_0 \gg 1$

Anisotropic diff. in *isotropic* turbulence

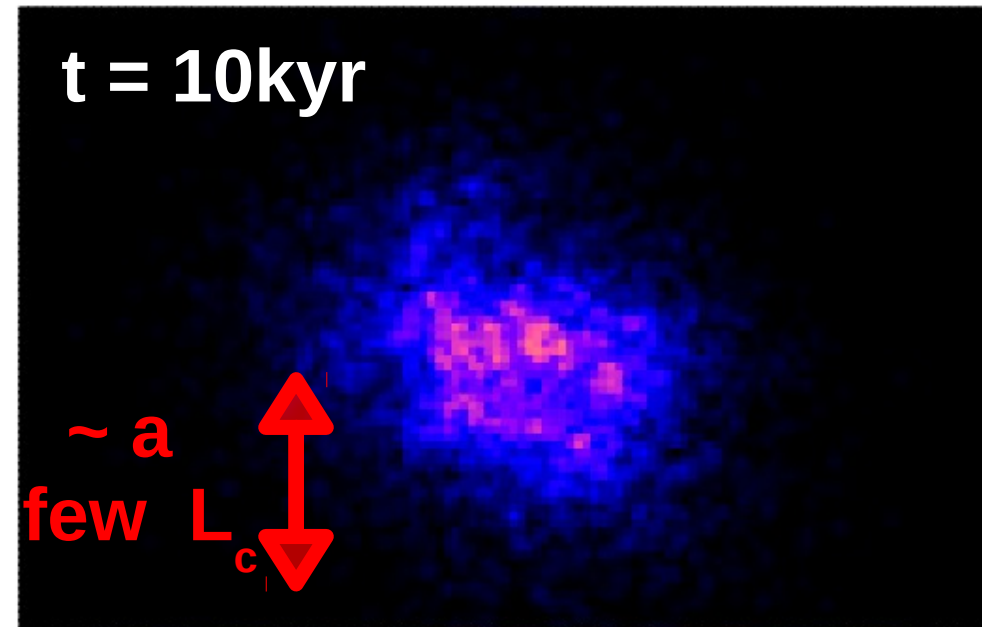
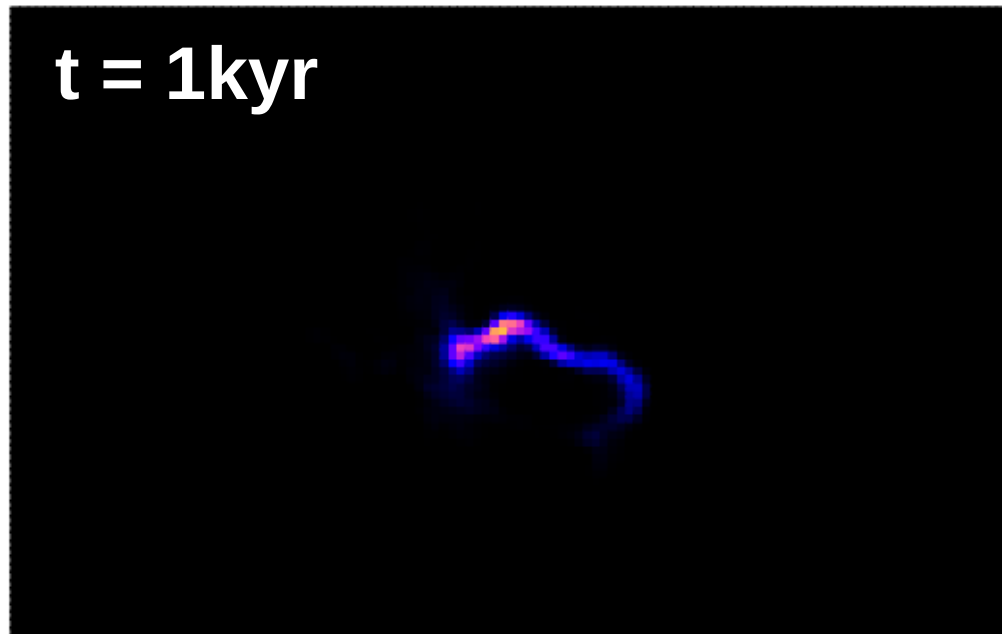
PRL **108**, 261101 (2012)

PHYSICAL REVIEW LETTERS

week ending
29 JUNE 2012

Filamentary Diffusion of Cosmic Rays on Small Scales

G. Giacinti,¹ M. Kachelrieß,¹ and D. V. Semikoz^{2,3}



$E/Z = 1$ PeV, Kolmogorov spectrum,
 $L_{max} = 150$ pc, Plot size : 400 pc

... then starts to tend
towards the $r \propto t^{1/2}$
behaviour.

The Galactic turbulent magnetic field

Satisfies: $\langle \mathbf{B}(\mathbf{x}) \rangle = \mathbf{0}$, $\langle \mathbf{B}(\mathbf{x})^2 \rangle = B_{\text{rms}}^2$

Power spectrum (if iso.): $\mathcal{P}(k) \propto k^{-\alpha}$ (e.g. $\alpha = 5/3, 3/2$)
for $2\pi/L_{\text{max}} \leq k \leq 2\pi/L_{\text{min}}$ with $L_{\text{min}} < 1 \text{ AU}$, $L_{\text{max}} \sim \text{few-100 pc}$

Fourier transform: $B_i(\mathbf{x}) = \int \frac{d^3k}{(2\pi)^3} B_i(\mathbf{k}) e^{i(\mathbf{k} \cdot \mathbf{x} + \phi_i(\mathbf{k}))}$
with $|\mathbf{B}(\mathbf{k})|^2 \propto k^{-\alpha-2}$

Coherence length: $\int_{-\infty}^{\infty} dL \langle \mathbf{B}(0) \cdot \mathbf{B}(\mathbf{x}(L)) \rangle \equiv L_c B_{\text{rms}}^2$

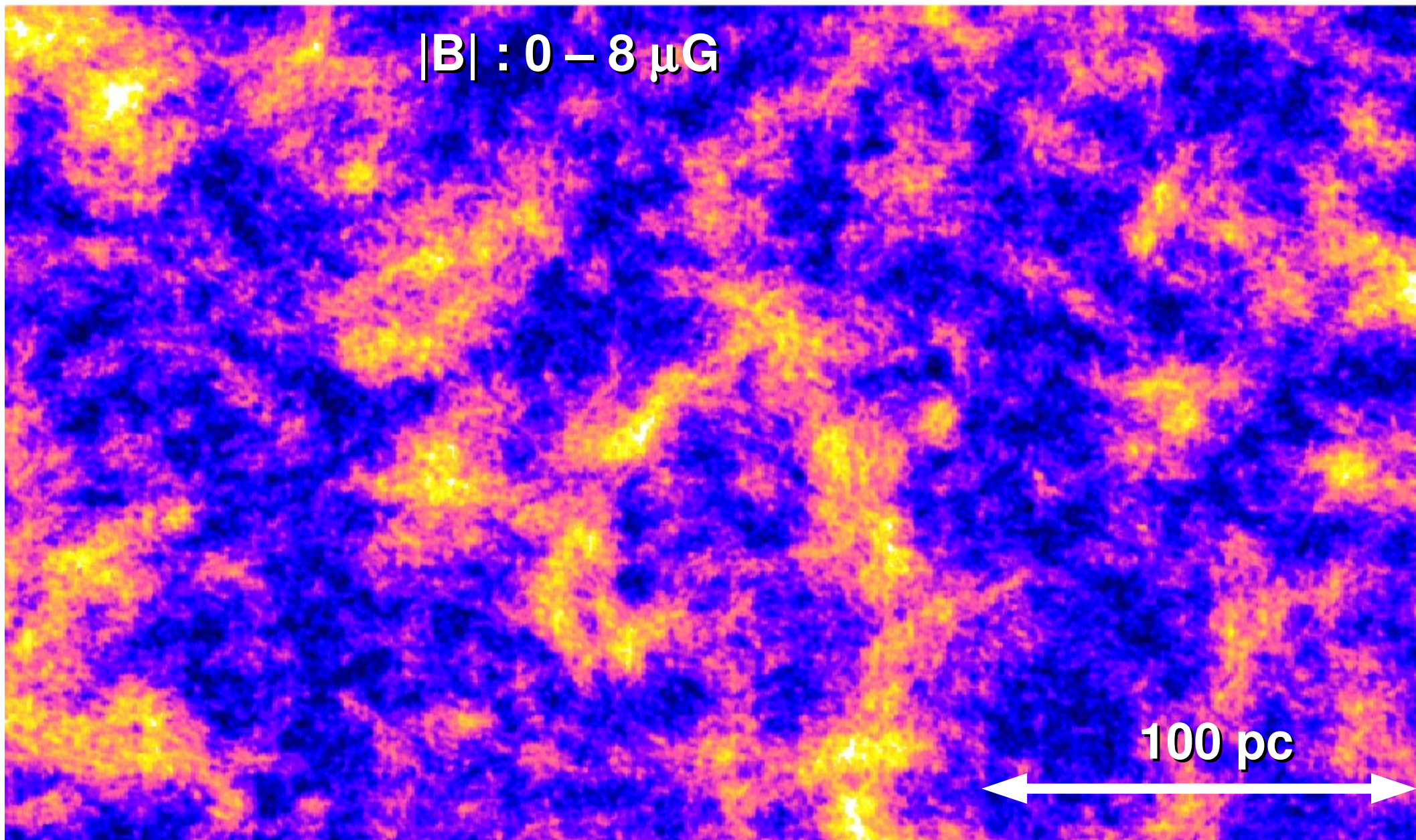
$$\Rightarrow L_c = \frac{1}{2} L_{\text{max}} \frac{n-1}{n} \frac{1 - (L_{\text{min}}/L_{\text{max}})^n}{1 - (L_{\text{min}}/L_{\text{max}})^{n-1}} \sim 1 - 10 \text{ s pc}$$

$$r_L \ll L_c$$

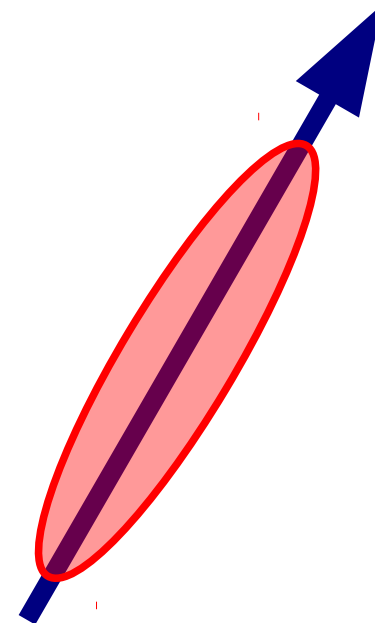
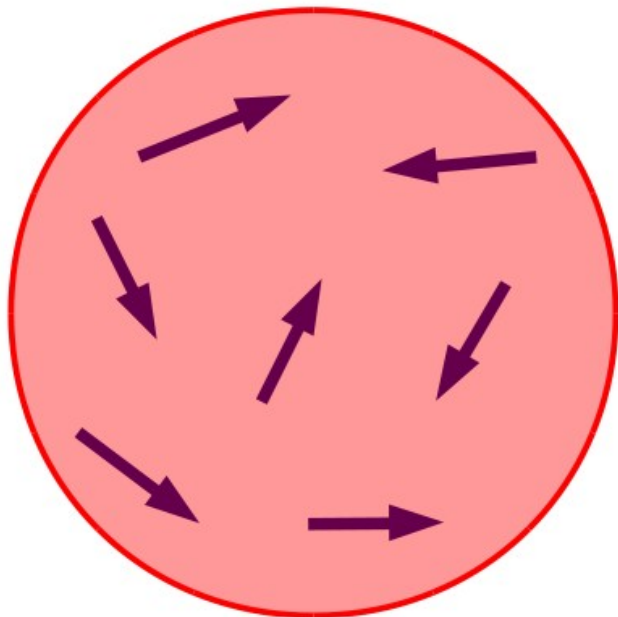
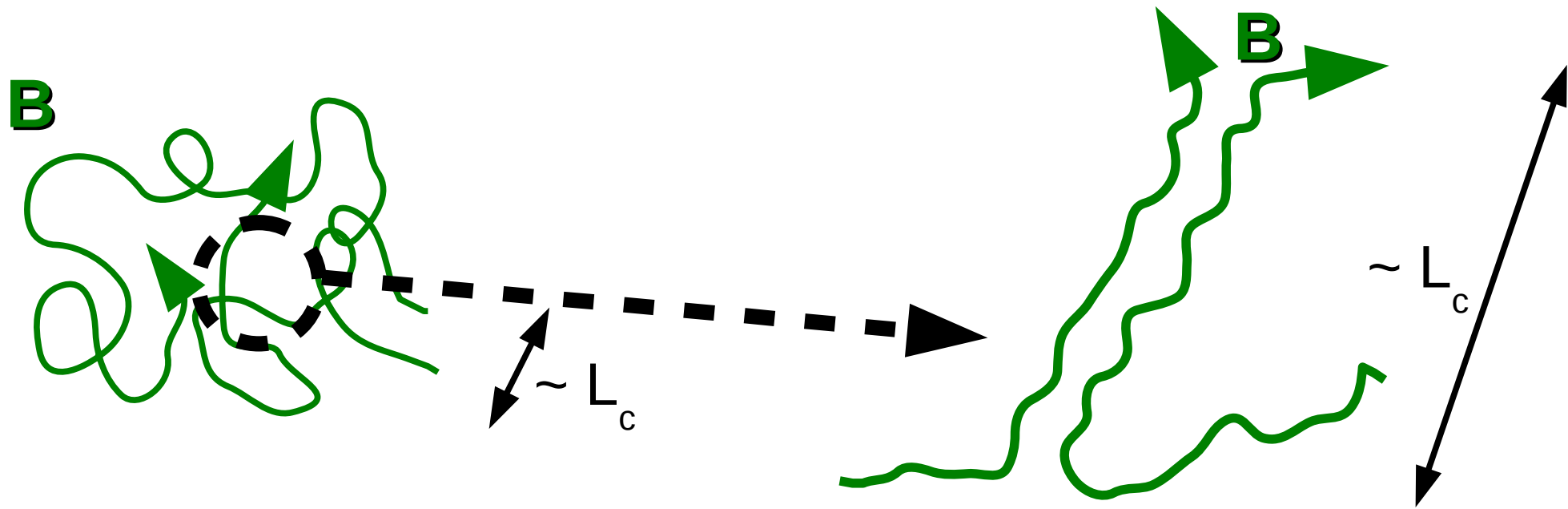
Kolmogorov turbulence

$|B| : 0 - 8 \mu\text{G}$

100 pc



Anisotropic diff. in *isotropic* turbulence

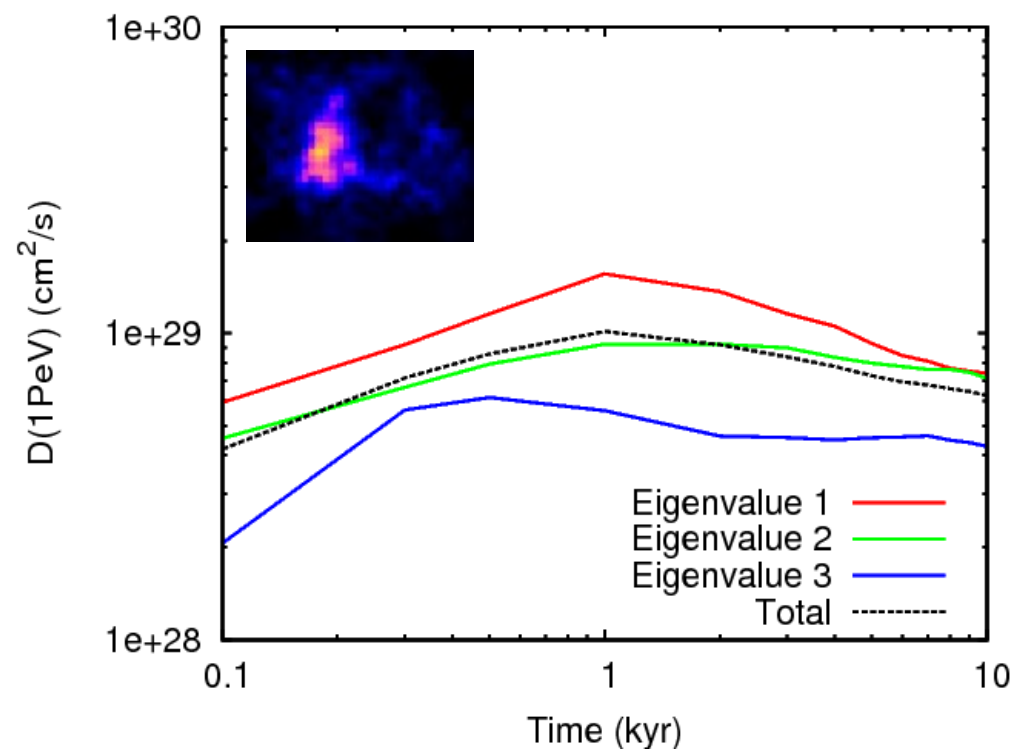
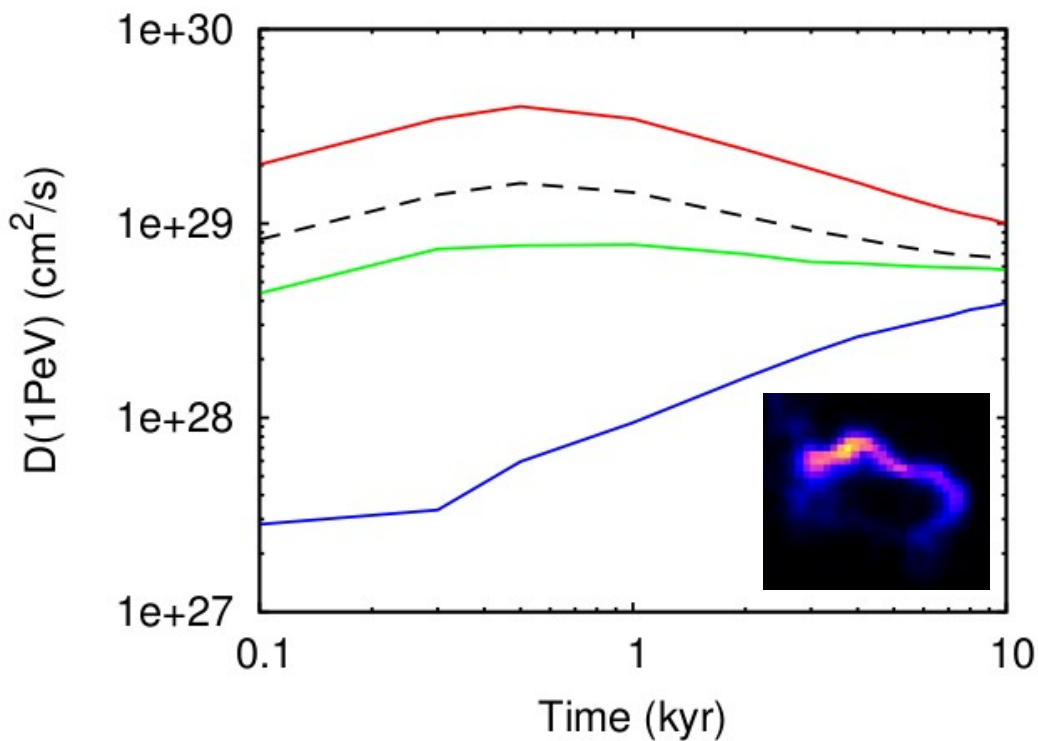


Eigenvalues of the diffusion tensor

Inject N particles at $\mathbf{x} = \mathbf{0}$ in **one single** B field realization ' b '

Calculate
$$D_{ij}^{(b)} = \frac{1}{N} \sum_{a=1}^N \frac{x_i^{(a)} x_j^{(a)}}{2t} \quad (i, j = X, Y, Z)$$

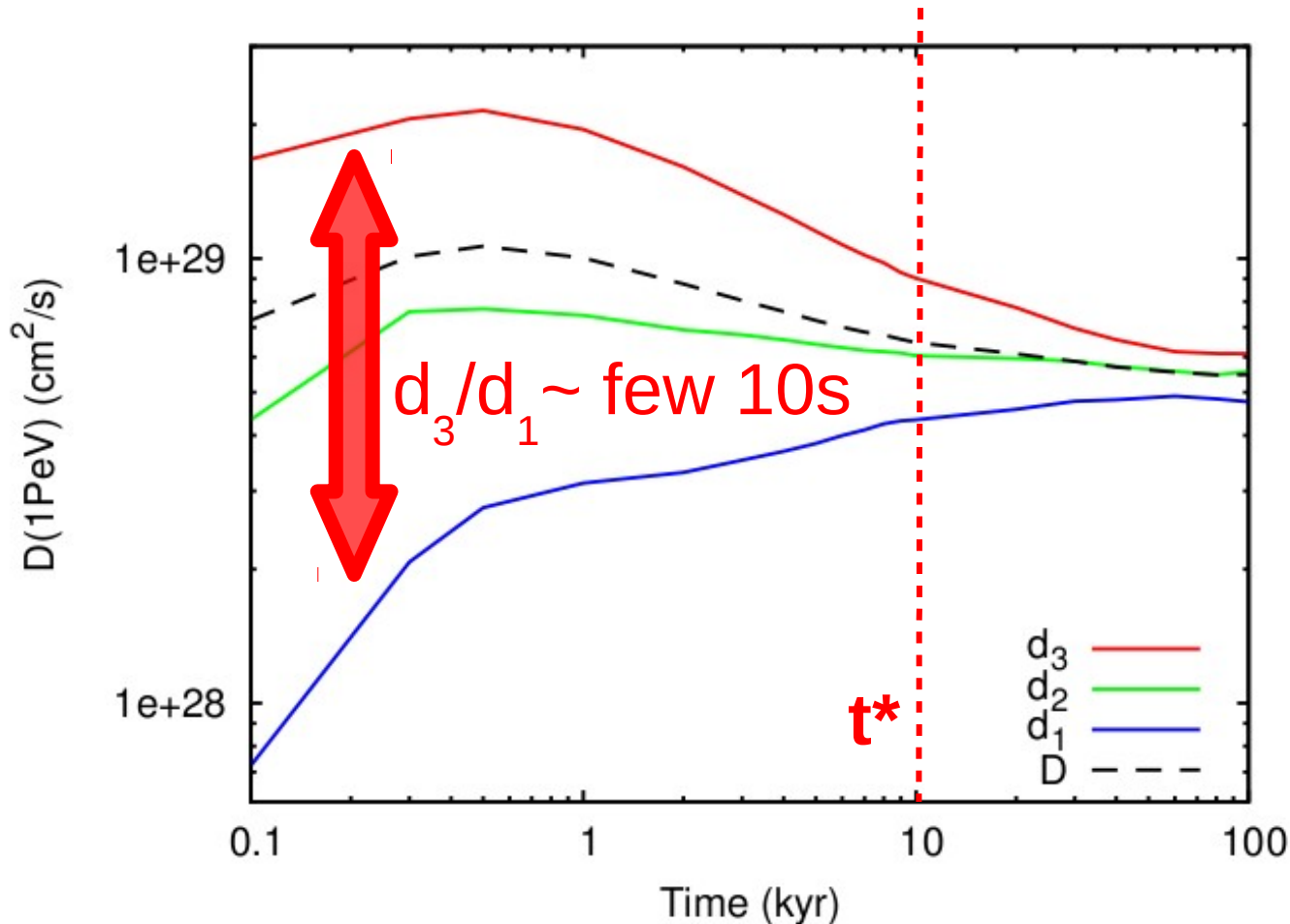
Compute its eigenvalues : $d_1^{(b)} < d_2^{(b)} < d_3^{(b)}$



Eigenvalues of the diffusion tensor

Average $d_i^{(b)}$ over M field realizations: $d_i = \frac{1}{M} \sum_{b=1}^M d_i^{(b)}$

($i=1,2,3$)



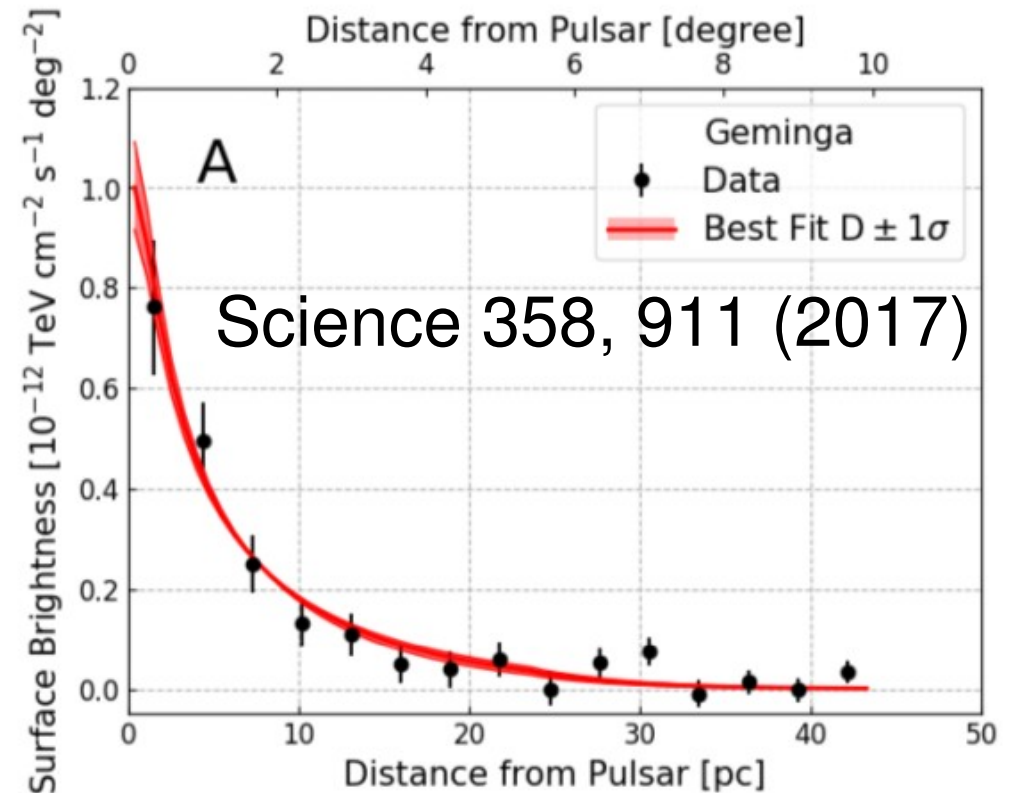
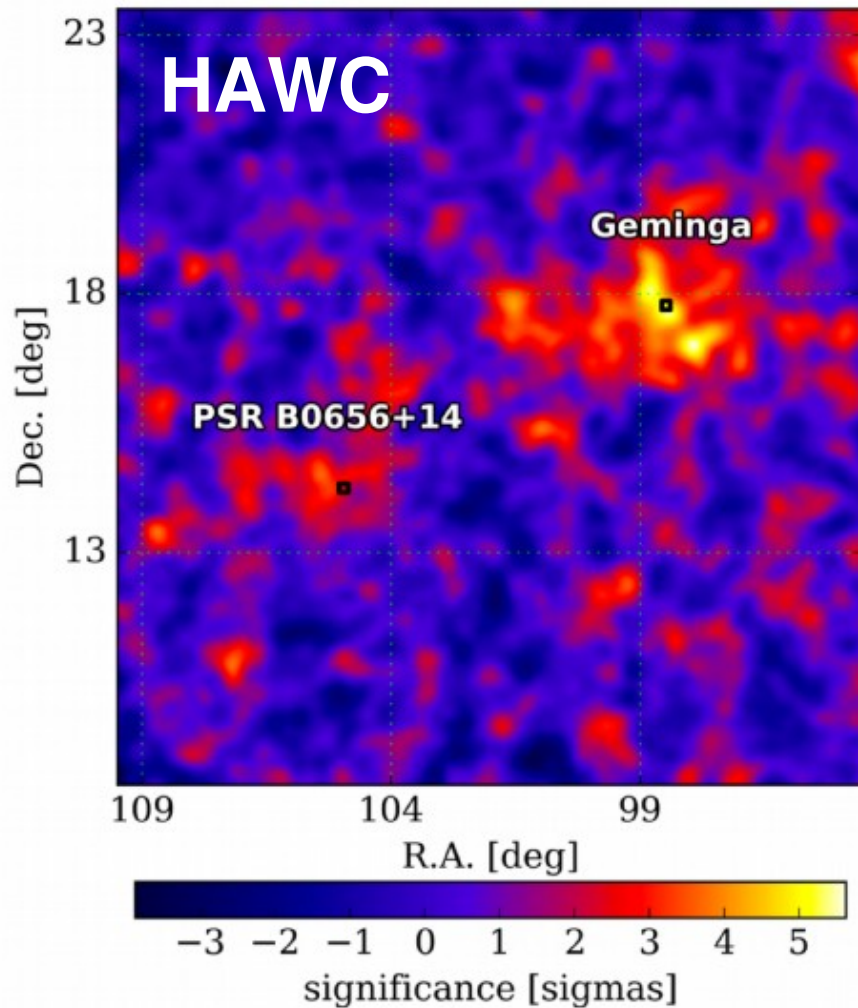
$$t_* \sim \underline{10^4 \text{ yr}} (l_{\text{max}}/150 \text{ pc})^\beta (E/\text{PeV})^{-\gamma} (B_{\text{rms}}/4 \mu\text{G})^\gamma$$

with $\beta \simeq 2$ and $\gamma = 0.25\text{--}0.5$

I – Extended gamma-ray emission around Geminga

Lopez-Coto & GG, MNRAS 479, 4526 (2018) [arXiv:1712.04373]

HAWC observations of Geminga region

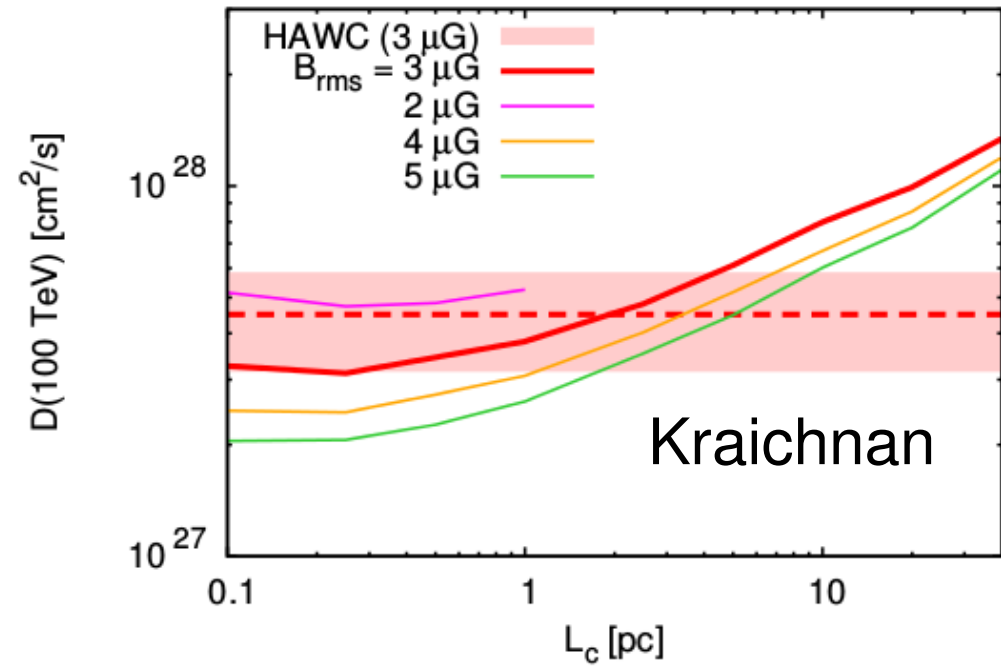
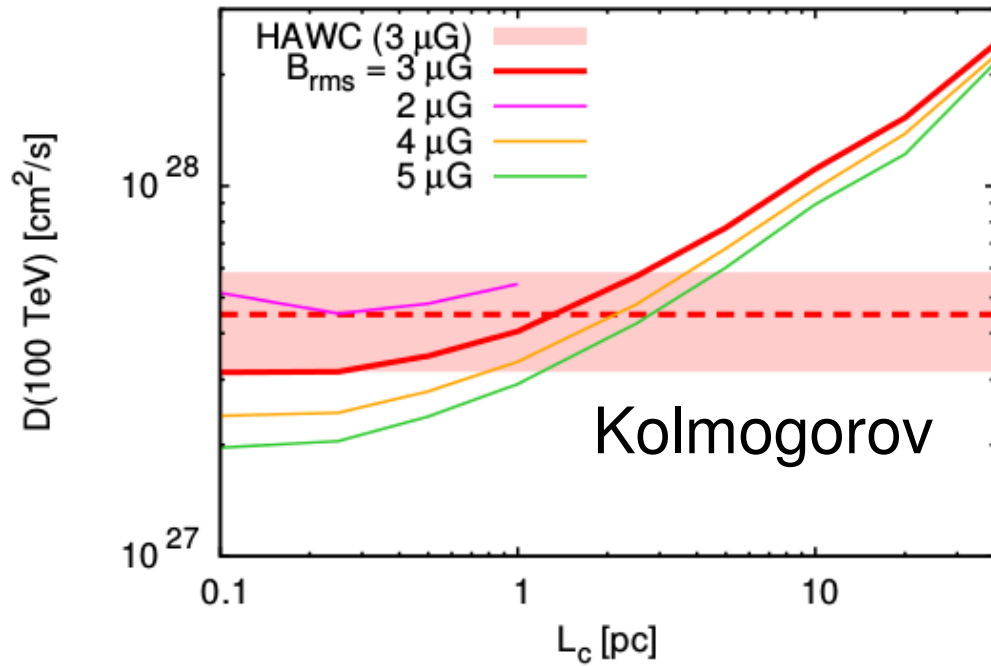


$$B = 3 \mu\text{G}$$

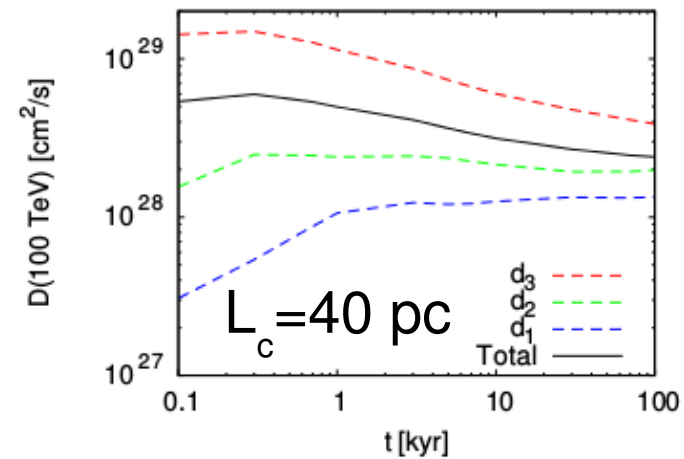
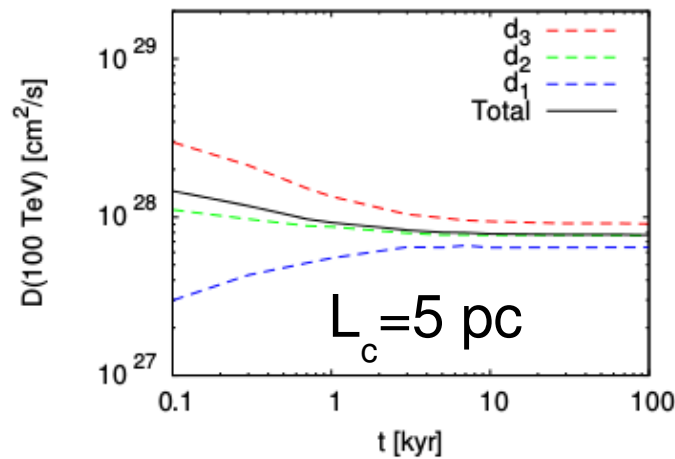
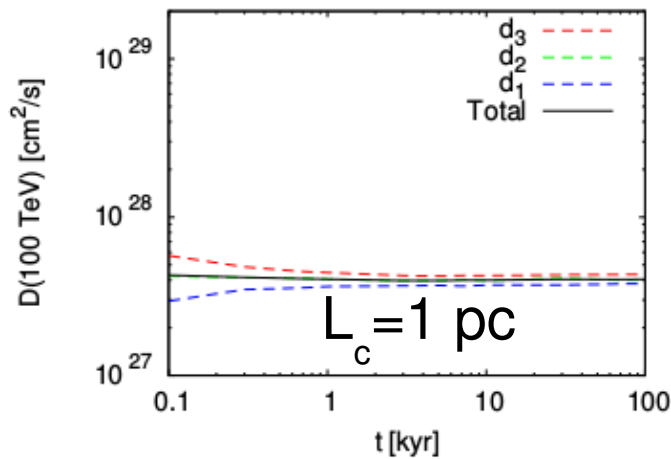
$$D_{100} = (4.5 \pm 1.2) \times 10^{27} \text{ cm}^2 \text{ s}^{-1} \text{ at } 100 \text{ TeV.}$$

If emission \sim symmetric: Can already put upper limits on the coherence length of the turbulence

100 TeV protons



Eigenvalues (Kolmogorov spectrum, $B_{\text{rms}} = 3 \mu\text{G}$):



Simulations

→ Inject 5000 electrons (40 – 500 TeV) :

$$dN/dE = f_e(E/E_0)^{-\alpha} \text{ with } \alpha = 2.24$$

→ Propagate in 3D realizations of B turbulence :

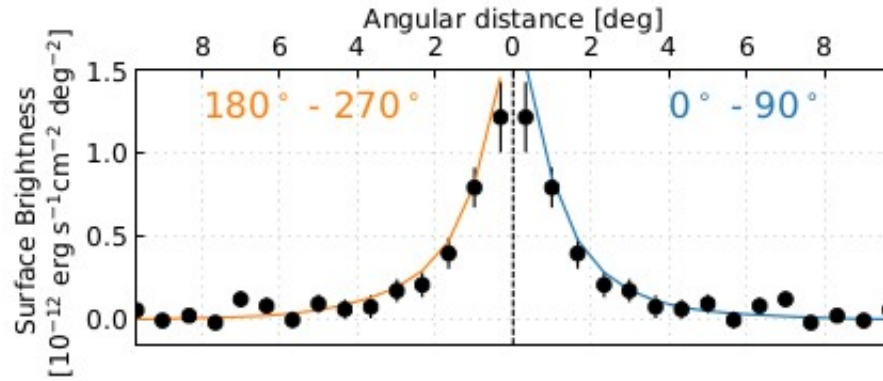
$$(62 \times 10 \text{ cases}) : \{ \mathcal{P}(k), L_c, B_{\text{rms}} \} \quad B_{\text{rms}} \equiv \sqrt{\langle B^2 \rangle}$$

→ Synchrotron + IC losses (/CMB) :

$$\left| \frac{dE}{dt} \right| \simeq 2.53 \times 10^{-15} \text{ TeV/s} \left[\left(\frac{B}{\mu\text{G}} \right)^2 + 10.1 \left(1 + \frac{E}{99 \text{ TeV}} \right)^{-1.5} \right] \left(\frac{E}{\text{TeV}} \right)^2$$

→ Calculate gamma-ray emission : IC on CMB photons.
(full Klein-Nishina treatment of the cross section)

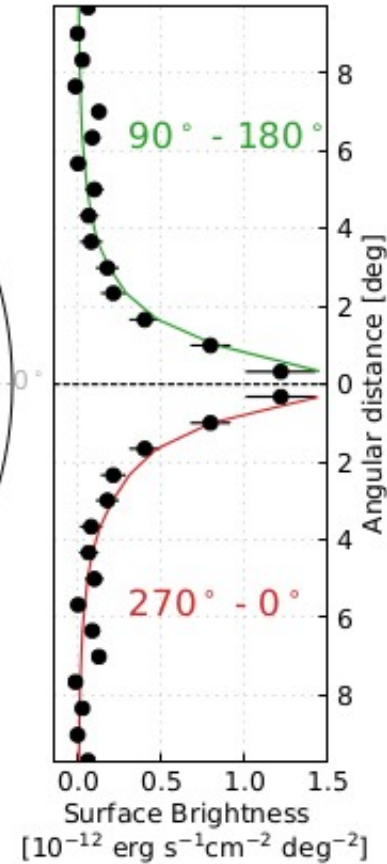
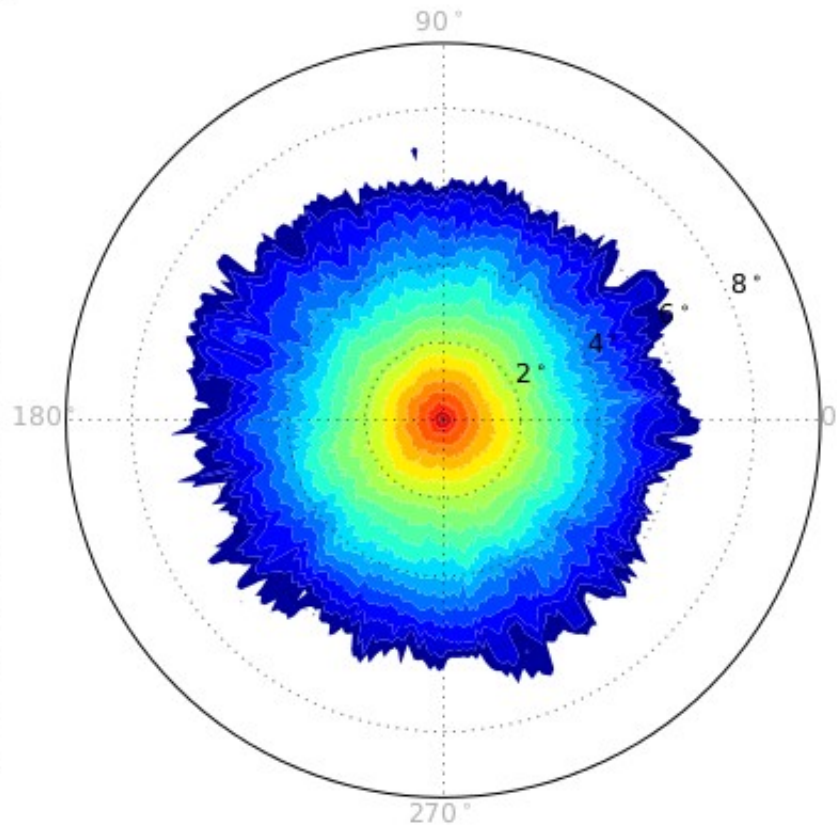
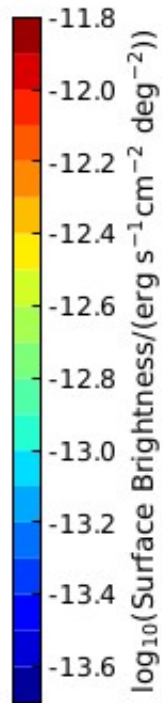
Predicted γ -ray surface brightness



Kolmogorov

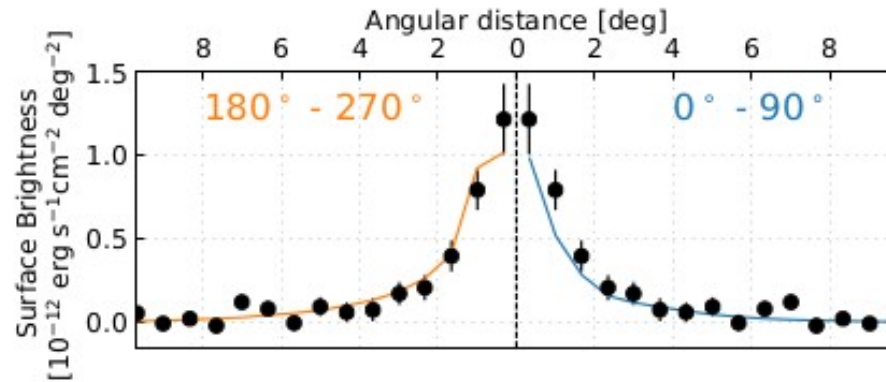
$$B_{\text{rms}} = 3 \mu\text{G}$$

$$L_c = 0.25 \text{ pc}$$



Predicted γ -ray surface brightness

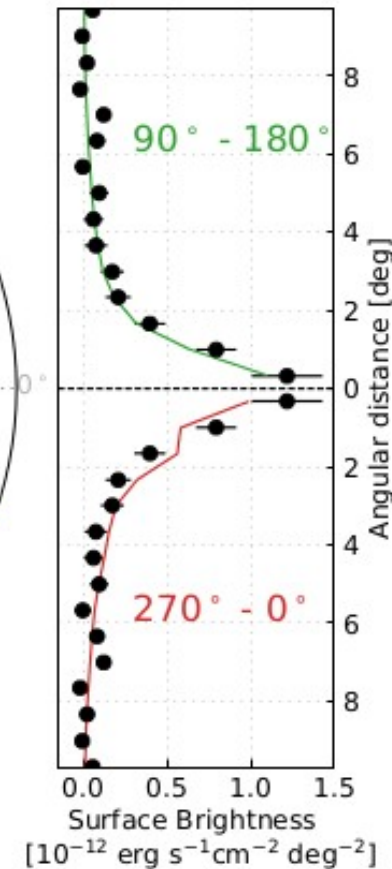
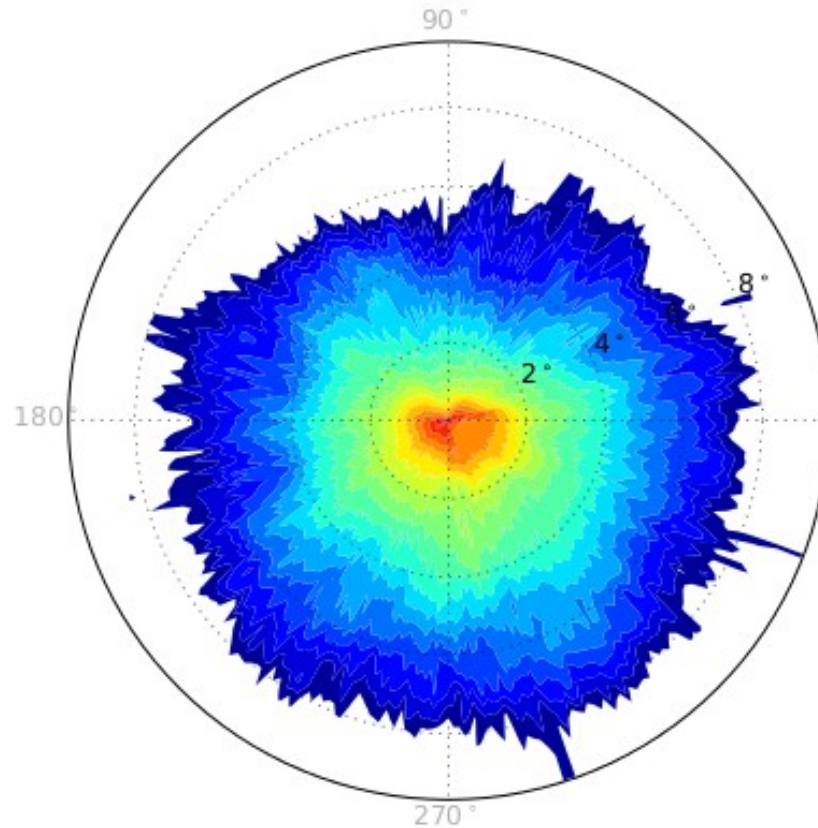
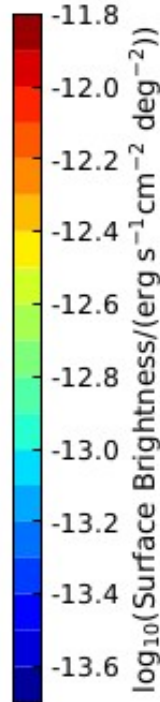
OK



Kolmogorov

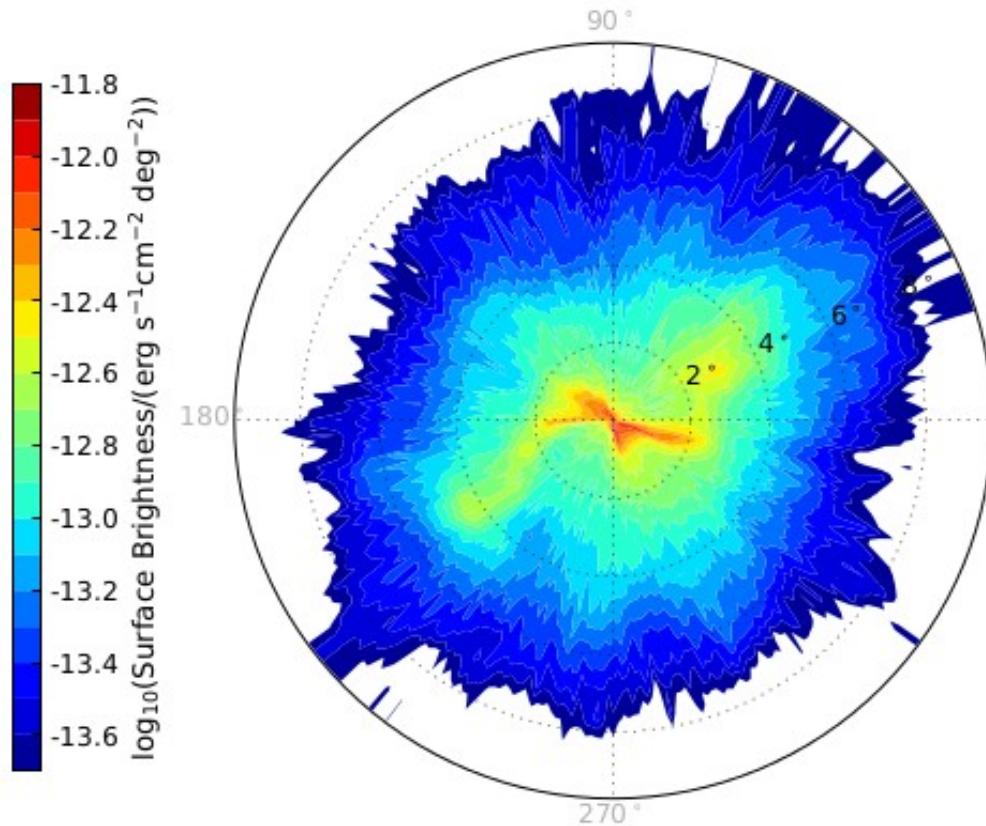
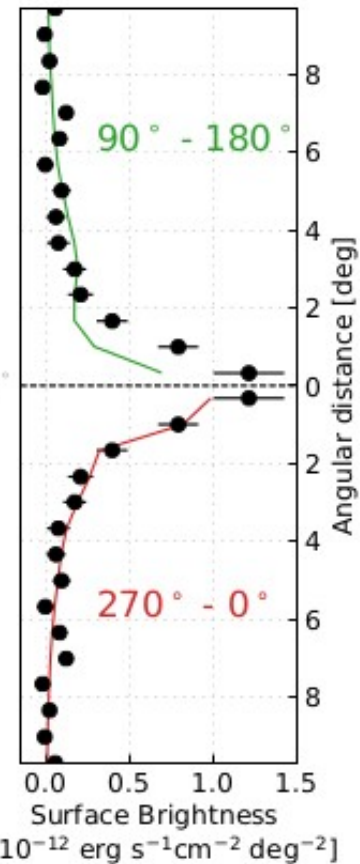
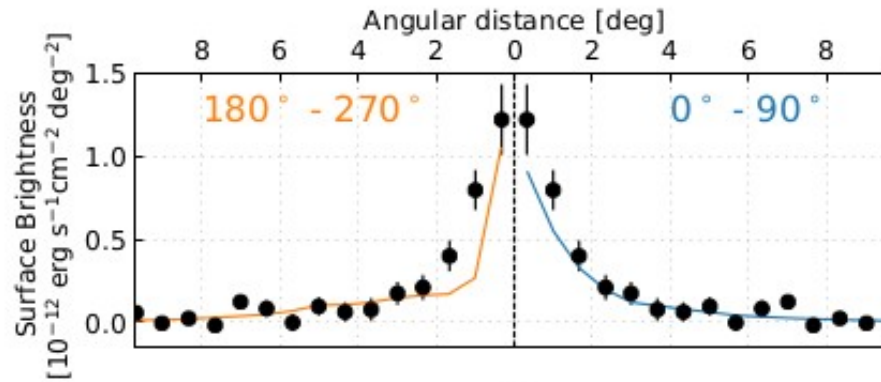
$$B_{\text{rms}} = 3 \mu\text{G}$$

$$L_c = 5 \text{ pc}$$



Predicted γ -ray surface brightness

**PERHAPS STILL
MARGINALLY
COMPATIBLE
WITH THE DATA?**

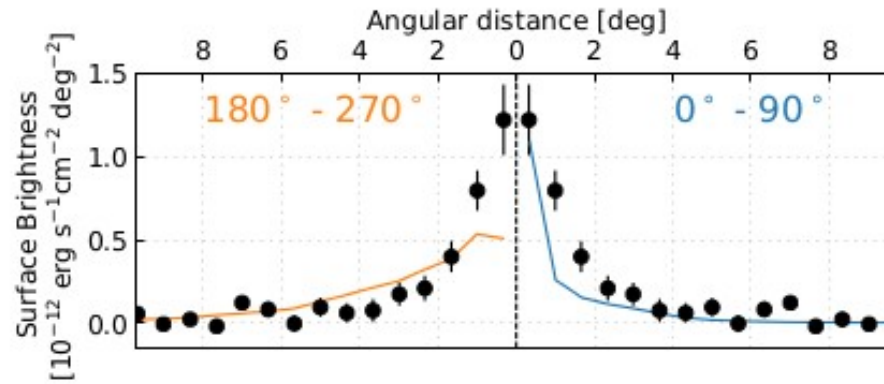


Kolmogorov

$$B_{\text{rms}} = 3 \mu\text{G}$$

$$L_c = 10 \text{ pc}$$

Predicted γ -ray surface brightness

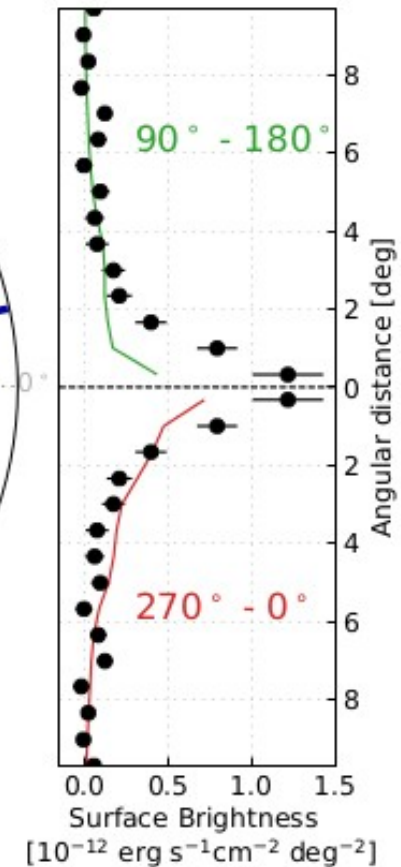
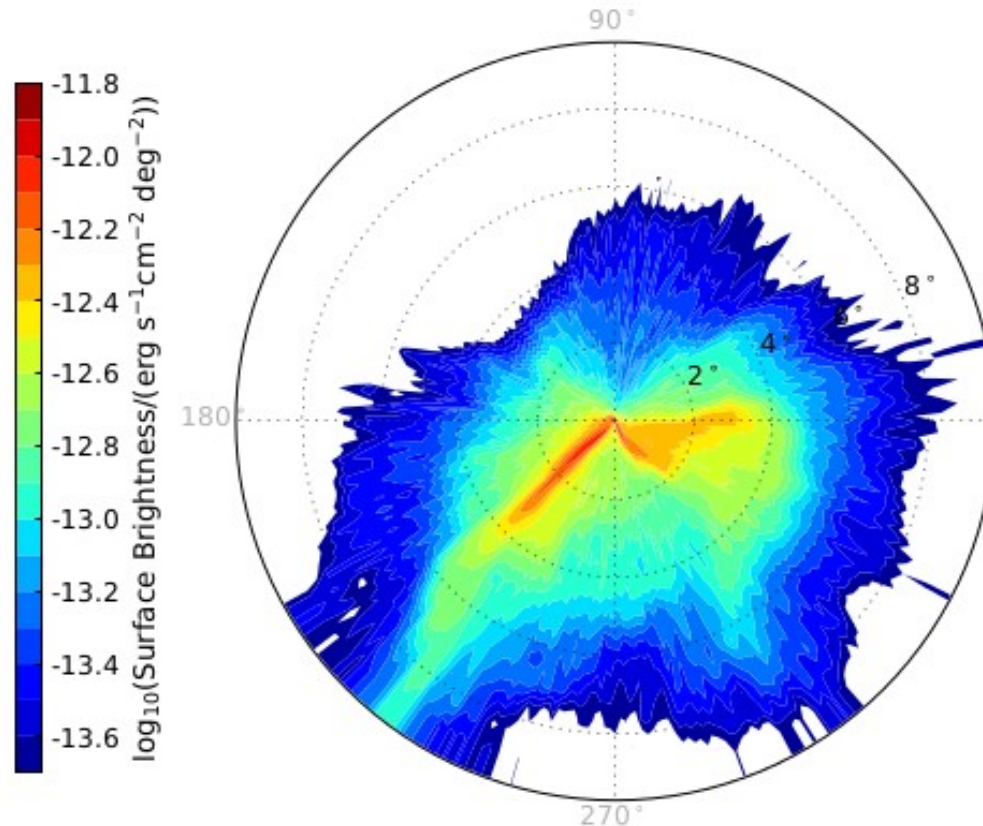


**INCOMPATIBLE
WITH THE DATA**

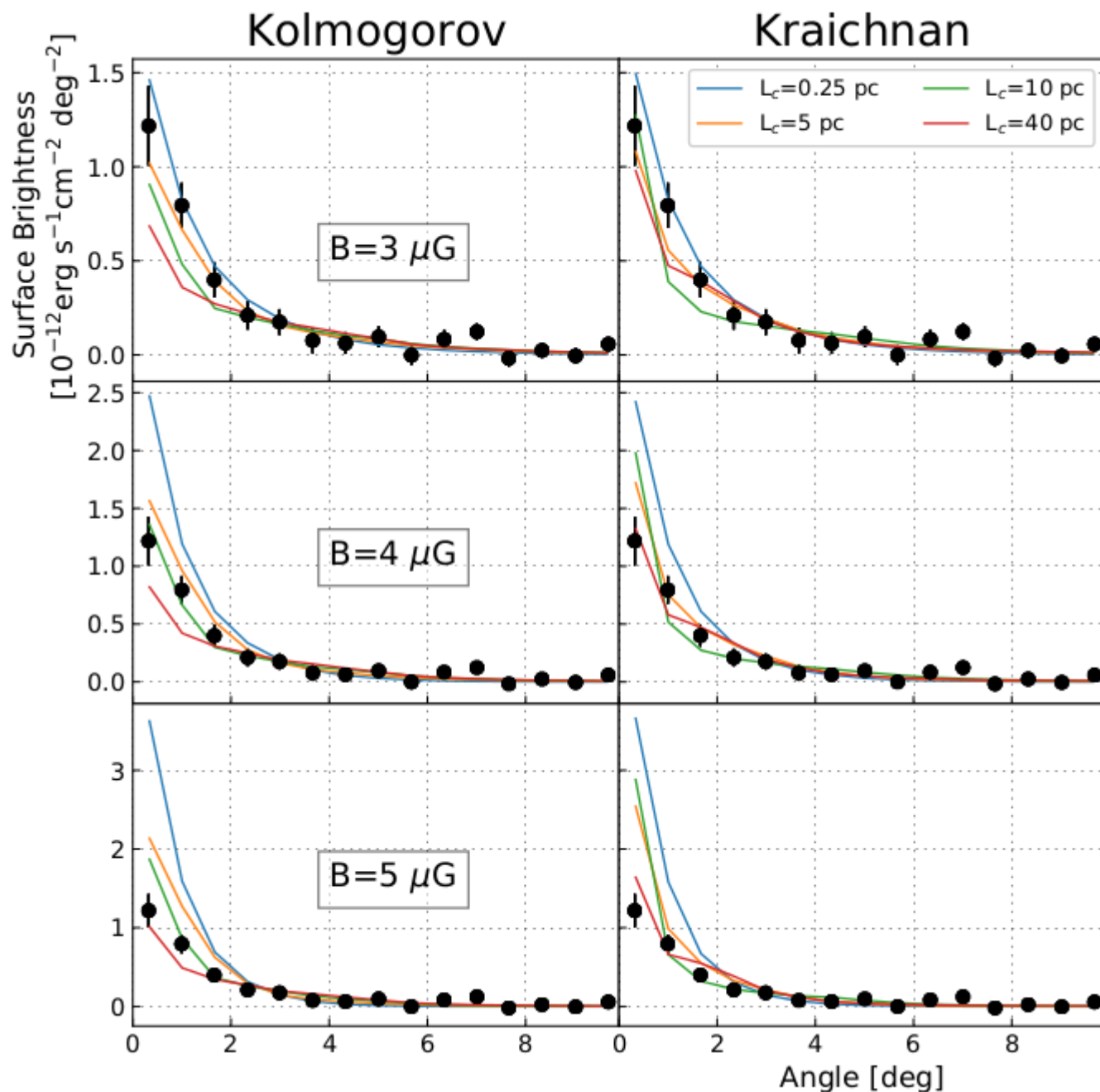
Kolmogorov

$$B_{\text{rms}} = 3 \mu\text{G}$$

$$L_c = 40 \text{ pc}$$

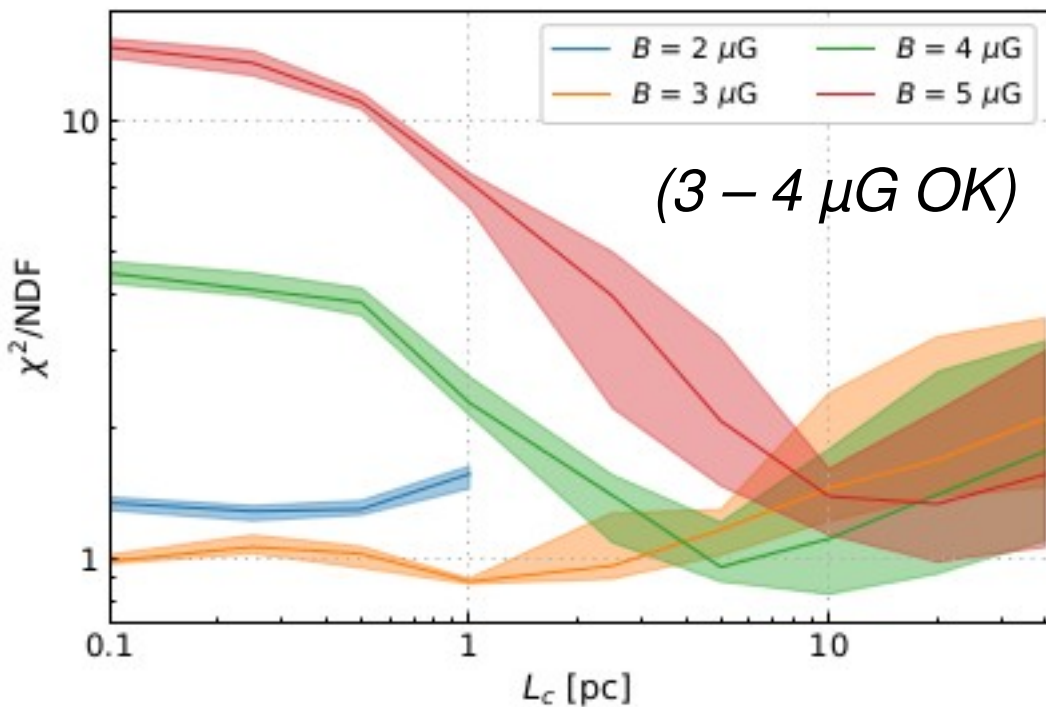


Surface brightness vs dist. to Geminga

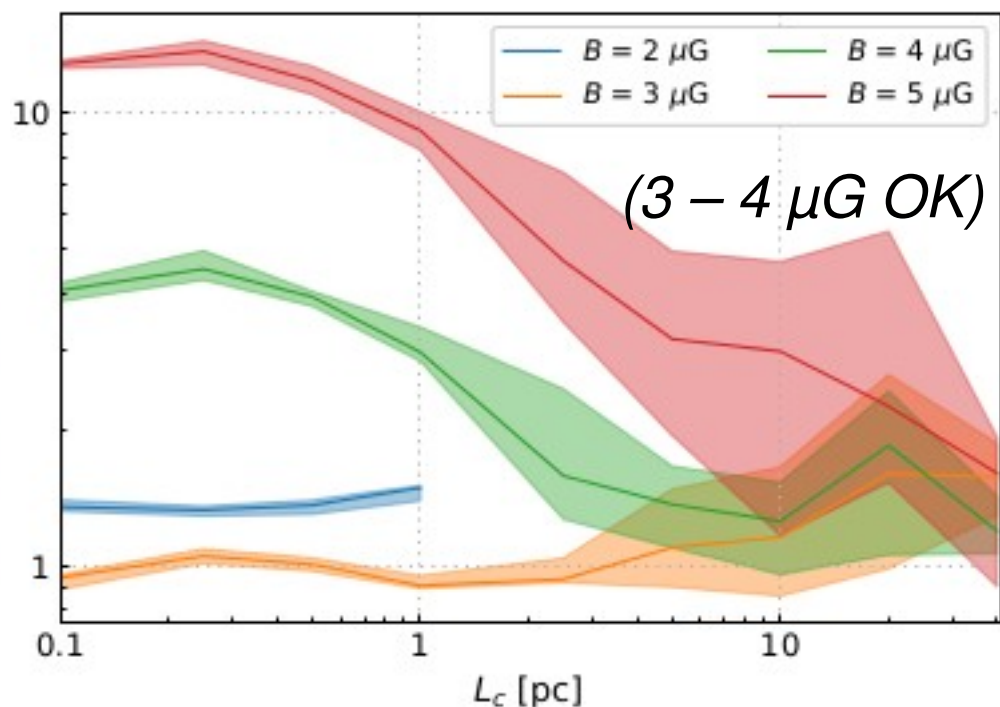


χ^2/ndf as a function of L_c

Kolmogorov



Kraichnan



Kolmogorov	2 μG	3 μG	4 μG	5 μG
0.1 pc	20.1/15	14.8/15	67.1/15	220/15
0.25 pc	19.2/15	15.9/15	61.6/15	203/15
0.5 pc	19.5/15	15.4/15	57.6/15	165/15
1 pc	23.4/15	13.3/15	34.0/15	108/15
2.5 pc	N/A	14.4/15	20.9/15	59.6/15
5 pc	N/A	17.5/15	14.4/15	30.9/15
10 pc	N/A	21.7/15	16.7/15	20.8/15
20 pc	N/A	25.2/15	21.0/15	20.0/15
40 pc	N/A	31.4/15	26.4/15	23.4/15

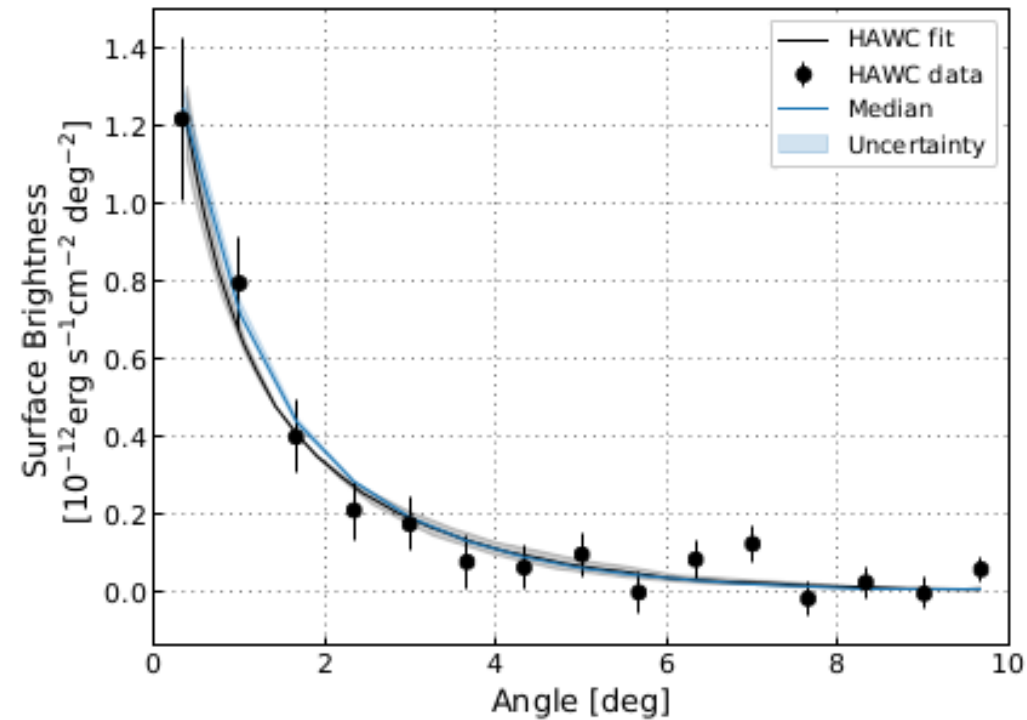
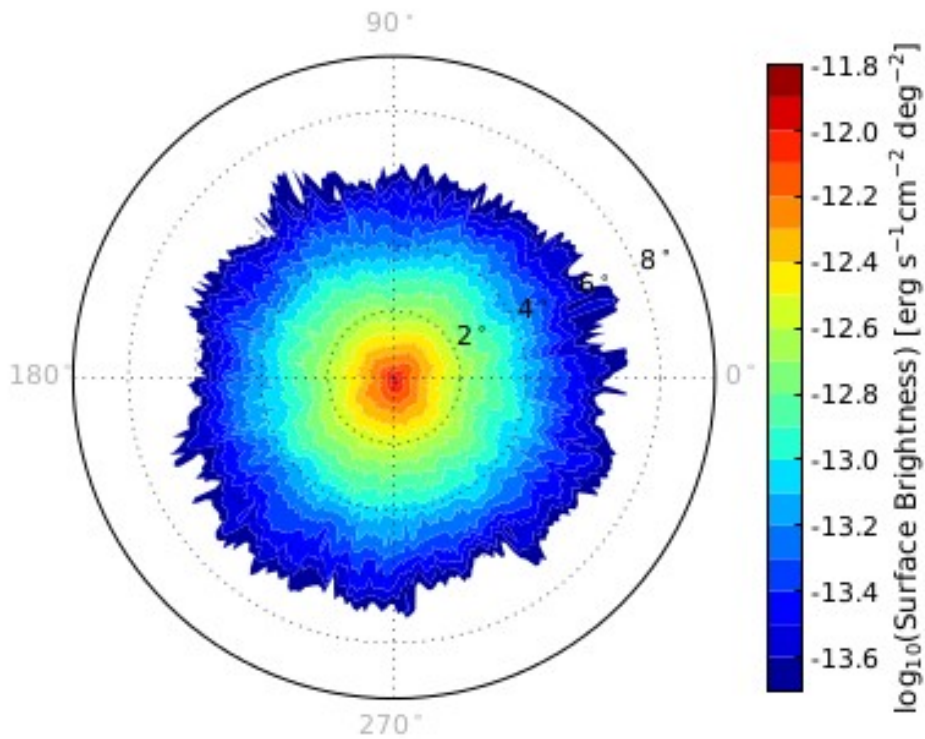
Kraichnan	2 μG	3 μG	4 μG	5 μG
0.1 pc	20.3/15	14.1/15	61.0/15	193/15
0.25 pc	20.0/15	15.8/15	67.9/15	205/15
0.5 pc	20.5/15	15.1/15	59.0/15	177/15
1 pc	22.4/15	13.6/15	44.5/15	137/15
2.5 pc	N/A	14.1/15	23.8/15	70.8/15
5 pc	N/A	16.5/15	20.5/15	47.6/15
10 pc	N/A	17.4/15	18.8/15	44.7/15
20 pc	N/A	24.0/15	27.7/15	33.8/15
40 pc	N/A	23.6/15	18.0/15	24.0/15

Our best fit to HAWC measurements

Kolmogorov
(Kraichnan)

$$B_{\text{rms}} = 3 \mu\text{G}$$

$$L_c = 1 \text{ pc}$$



Radio observations

Radio observations suggest that L_c in the spiral arms of our Galaxy is equal to only a few parsecs, which is very close to our best fit value. $L_{\max} = 5L_c$ for Kolmogorov turbulence) is ≤ 20 pc according to e.g.

Haverkorn et al., ApJ **680**, 362 (2008) :

ABSTRACT

We analyze Faraday rotation and depolarization of extragalactic radio point sources in the direction of the inner Galactic plane to determine the outer scale and amplitude of the rotation measure power spectrum. Structure functions of rotation measure show lower amplitudes than expected when extrapolating electron density fluctuations to large scales assuming a Kolmogorov spectral index. This implies an outer scale of those fluctuations on the order of a parsec, much smaller than commonly assumed. Analysis of partial depolarization of point sources independently indicates a small outer scale of a Kolmogorov power spectrum. In the Galaxy's spiral arms, no rotation measure fluctuations on scales above a few parsecs are measured. In the interarm regions fluctuations on larger scales than in spiral arms are present, and show power law behavior with a shallow spectrum. These results suggest that in the spiral arms stellar sources such as stellar winds or protostellar outflows dominate the energy injection for the turbulent energy cascade on parsec scales, while in the interarm regions supernova and super bubble explosions are the main sources of energy on scales on the order of 100 parsecs.

See also Iacobelli M et al A&A **558**, A72 (2013)

Part I: Conclusions and perspectives

- **"Anisotropic" propagation** of CRs in the ISM must be taken into account on scales $< \sim$ several L_c .
- **HAWC measurements for Geminga**
 - **Constraints on the surrounding turbulence.**
- **γ -ray observatories as a probe of :**
 - **Turbulent interstellar magnetic fields**
 - **Future : CR-driven instabilities around CR sources.**
- **Implications of a small D for B/C , all-electron spectrum.**

II – Anisotropic CR diffusion and Galactic magnetic field models

**GG, Kachelriess & Semikoz,
JCAP 07, 051 (2018) [arXiv:1710.08205]**

Isotropic diffusion

$$D_0 = (3 - 8) \times 10^{28} \text{ cm}^2/\text{s}$$

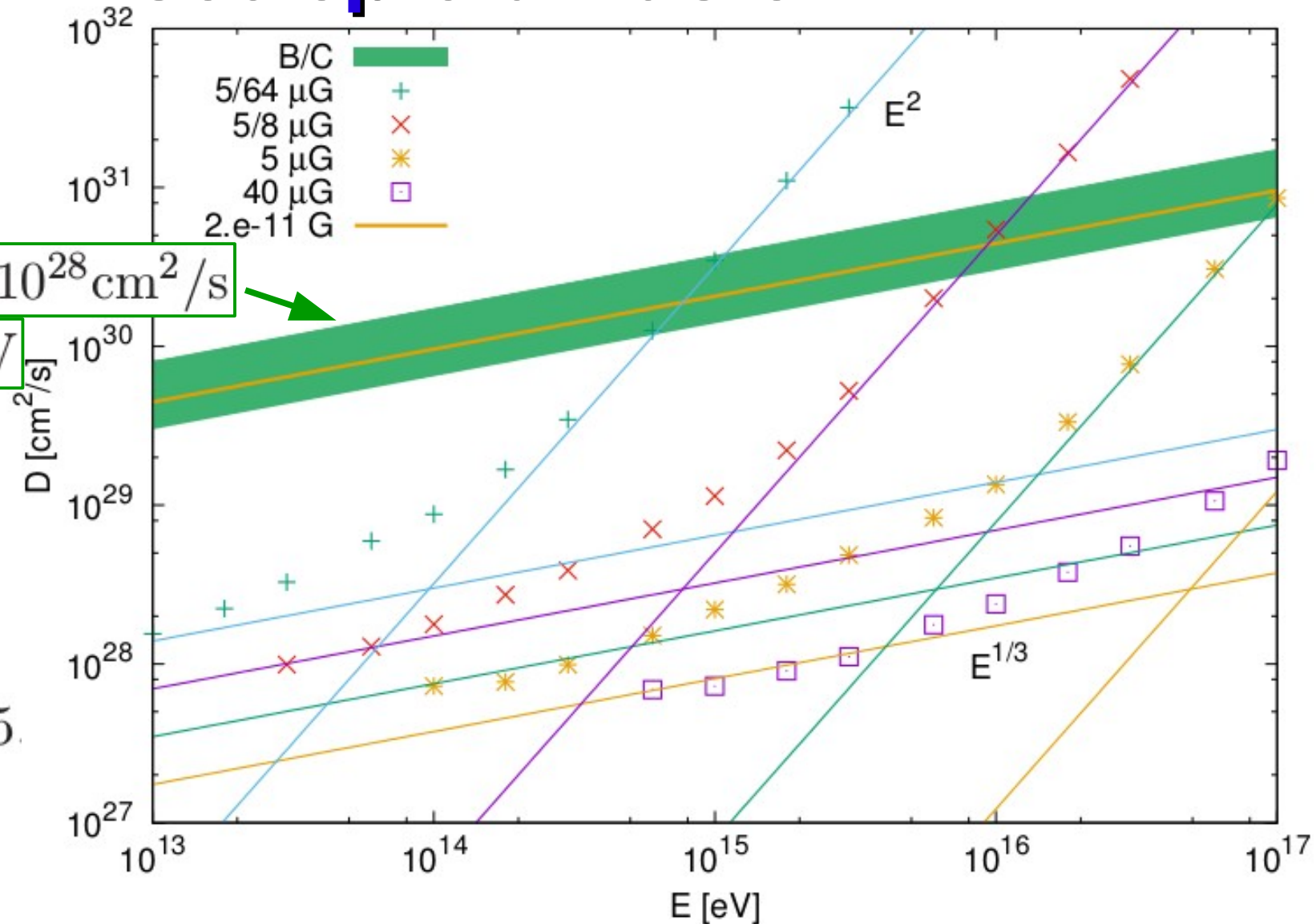
$$\text{at } E_0 = 10 \text{ GeV}$$

$$H \simeq 5 \text{ kpc}$$

$$\mathcal{P}(k) \propto k^{-5/3}$$

$$L_{\text{coh}} = L_{\text{max}}/5$$

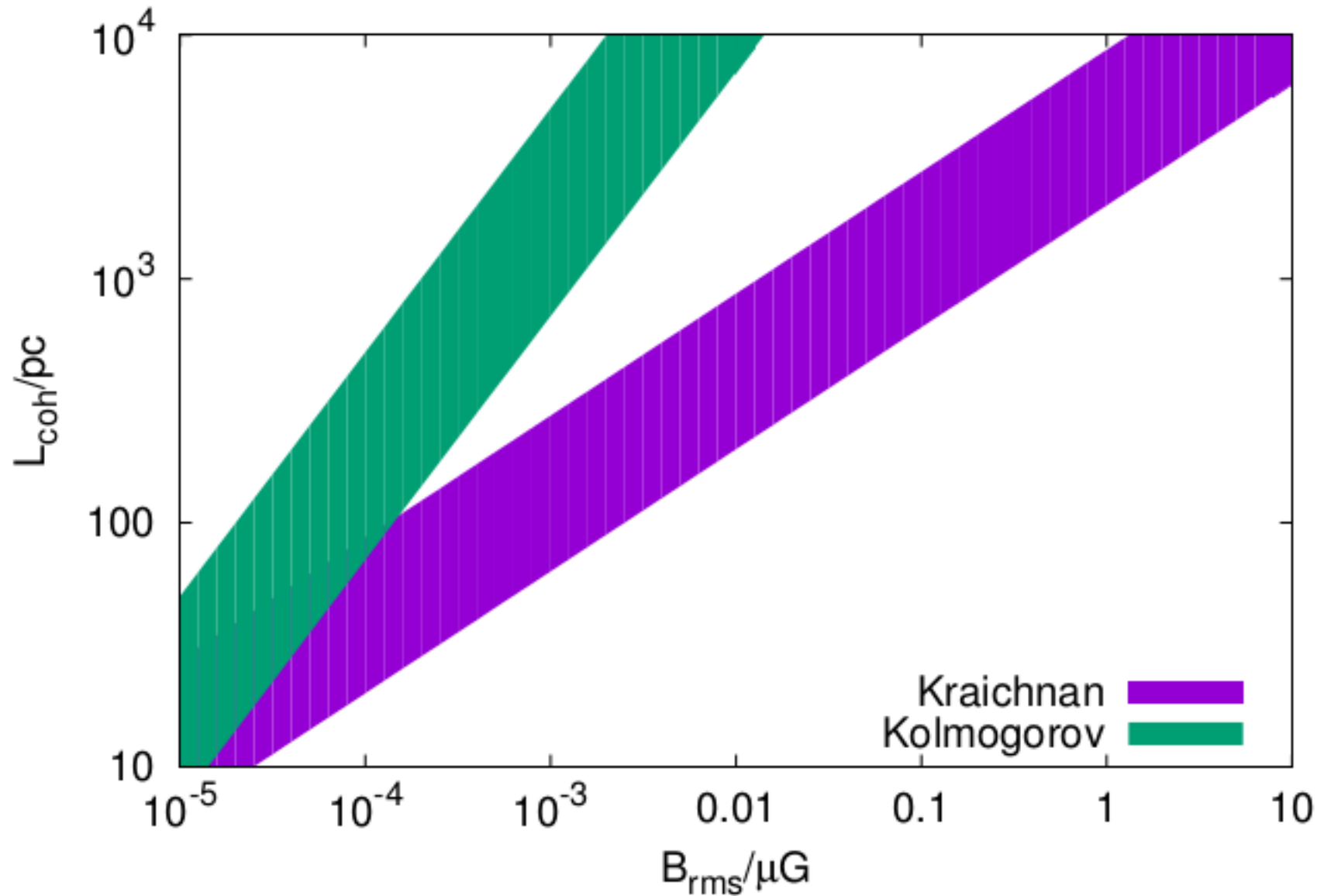
$$L_{\text{max}} = 25 \text{ pc}$$



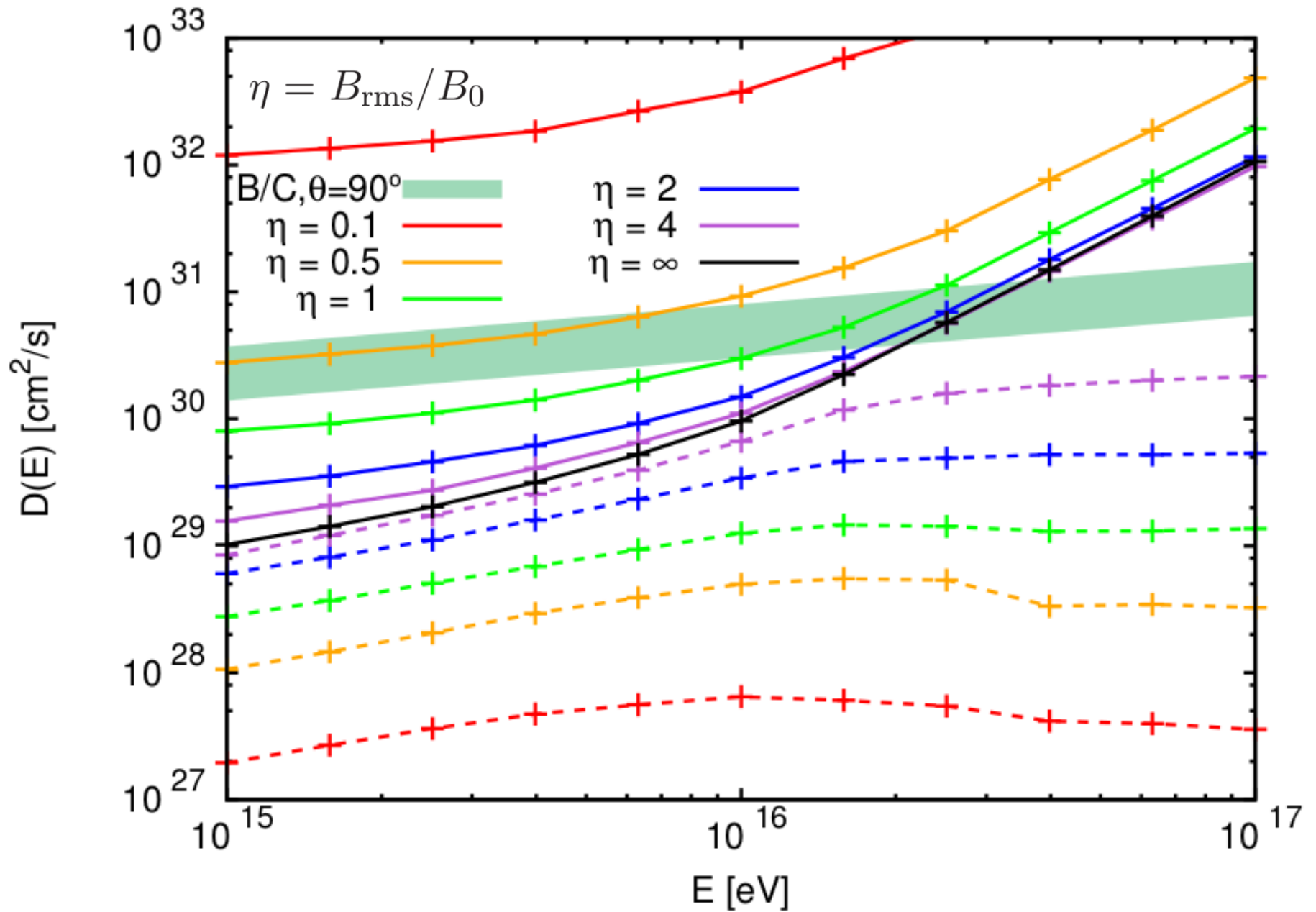
$$D = \frac{cL_0}{3} \left[(R_L/L_0)^{2-\alpha} + (R_L/L_0)^2 \right], \quad L_0 \simeq L_{\text{coh}}/(2\pi)$$

Isotropic diffusion

Allowed ranges of B_{rms} and L_{coh} compatible with $D_0 = (3-8) \times 10^{28} \text{ cm}^2/\text{s}$ at $E_0 = 10 \text{ GeV}$



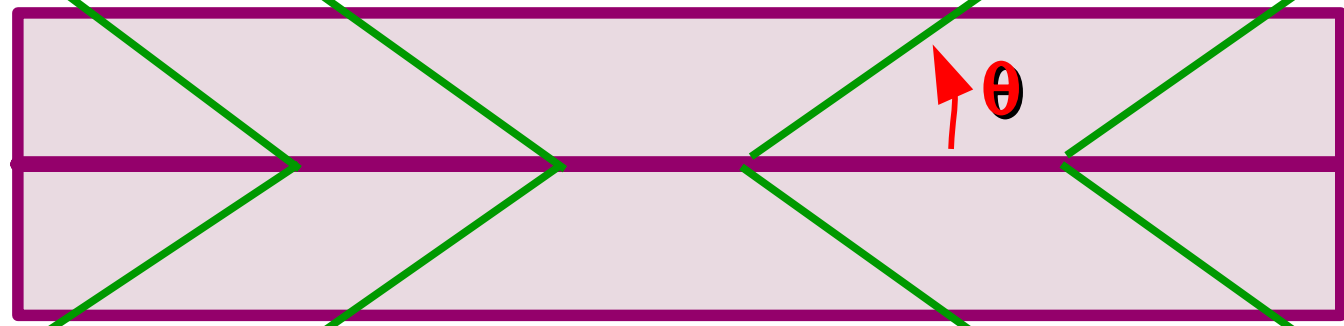
Anisotropic diffusion



$L_{\text{max}} = 100 \text{ pc}$

$B_{\text{tot}} = \sqrt{B_{\text{rms}}^2 + B_0^2} = 1 \mu\text{G}$

Grammage with an out-of-plane B

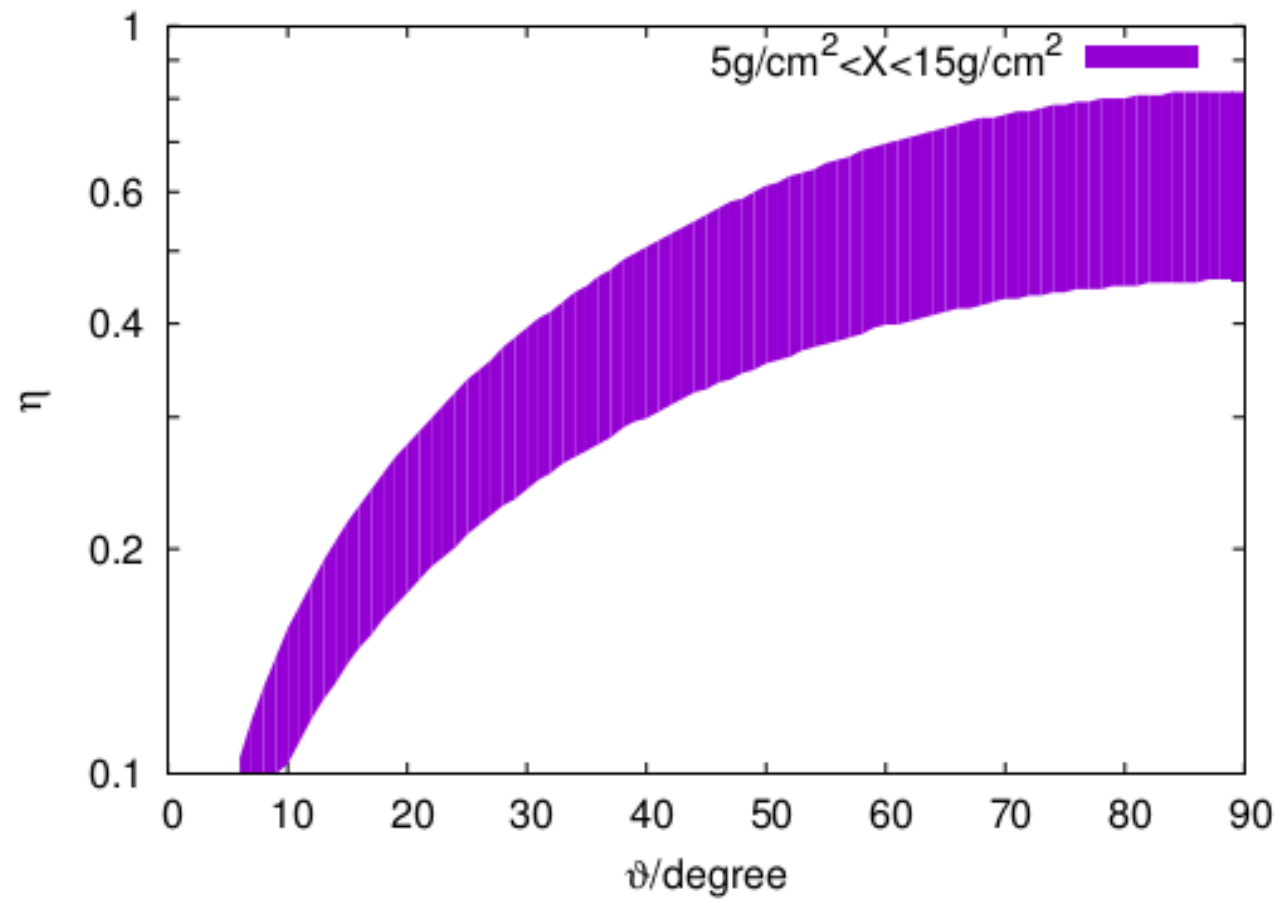


$H = 5 \text{ kpc}$

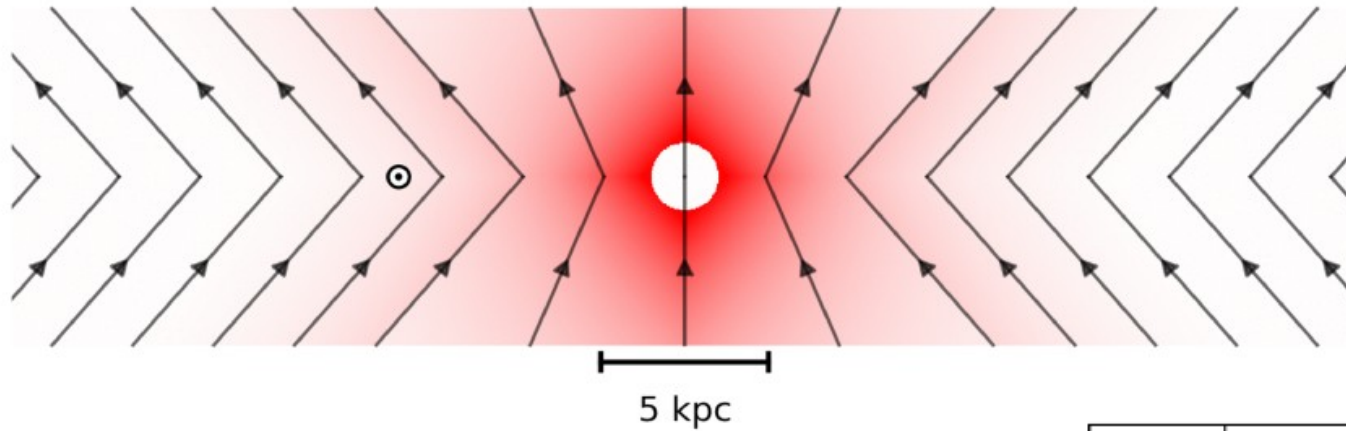
$\rho/m_p \simeq 1/\text{cm}^3 \quad h = 150 \text{ pc}$

$$X = c\rho hH/D_z$$

$$D_z = D_{\perp} \cos^2 \vartheta + D_{\parallel} \sin^2 \vartheta$$



Jansson & Farrar GMF model



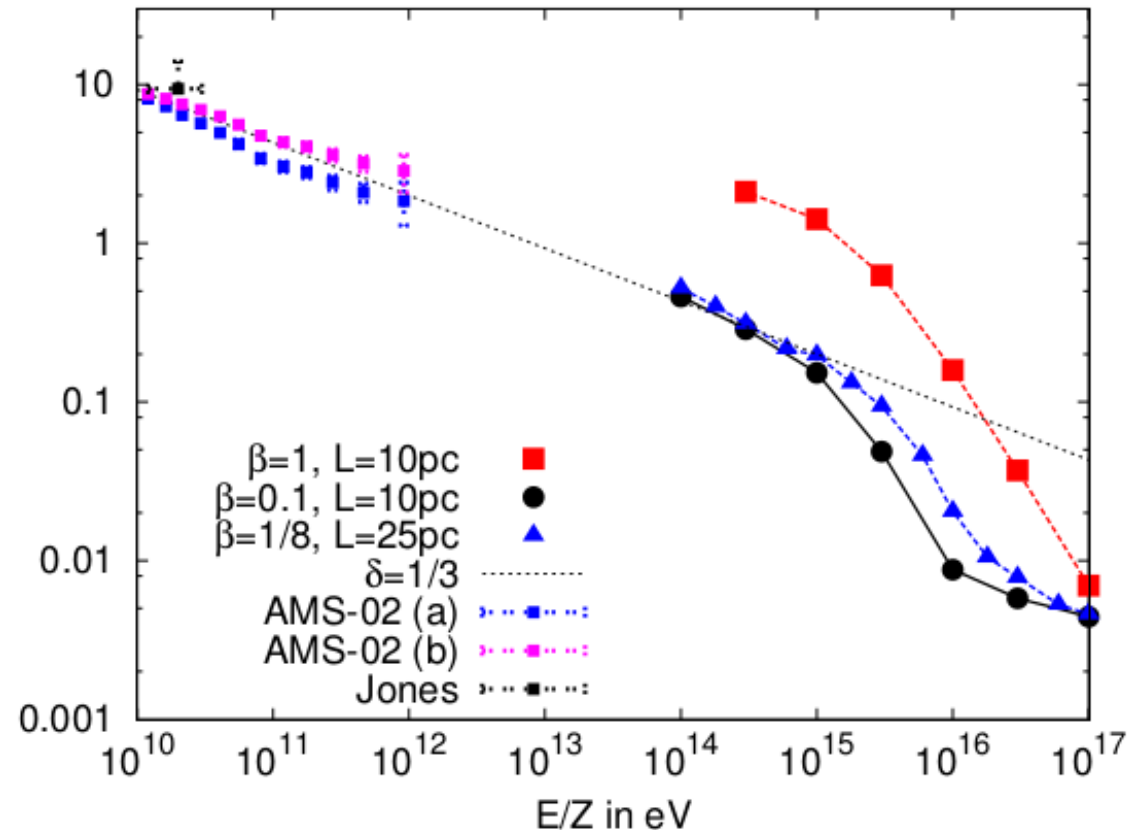
“X-field”

=> CRs go in the halo

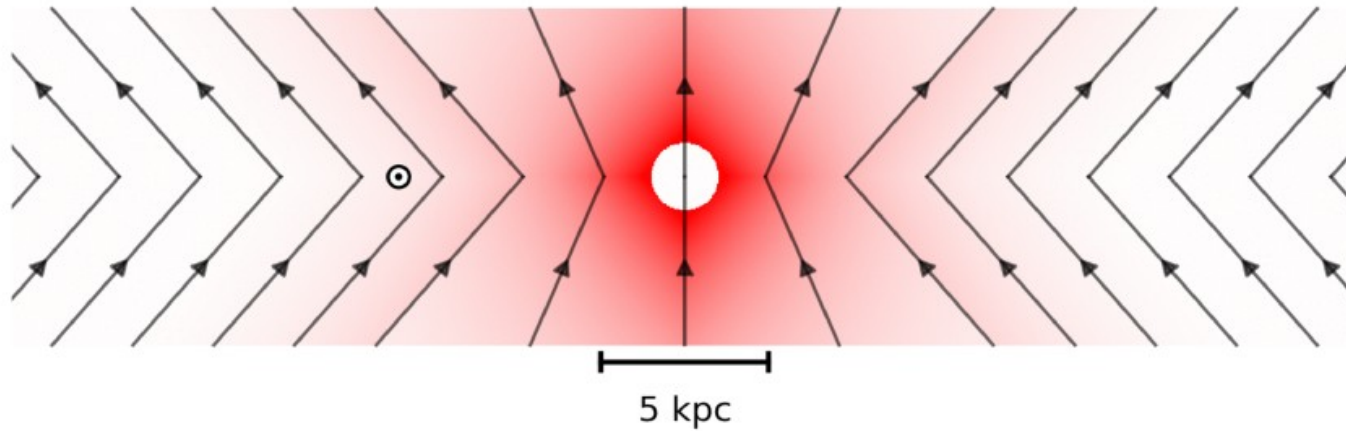
$X(E)$ reproduced if TF
reduced by a factor $\approx 8-10$ \rightarrow

(1) Avg turb. level $\eta \approx 0.25$
along CR trajectories

(2) typically, $\Theta \approx 20^\circ$



Jansson & Farrar GMF model



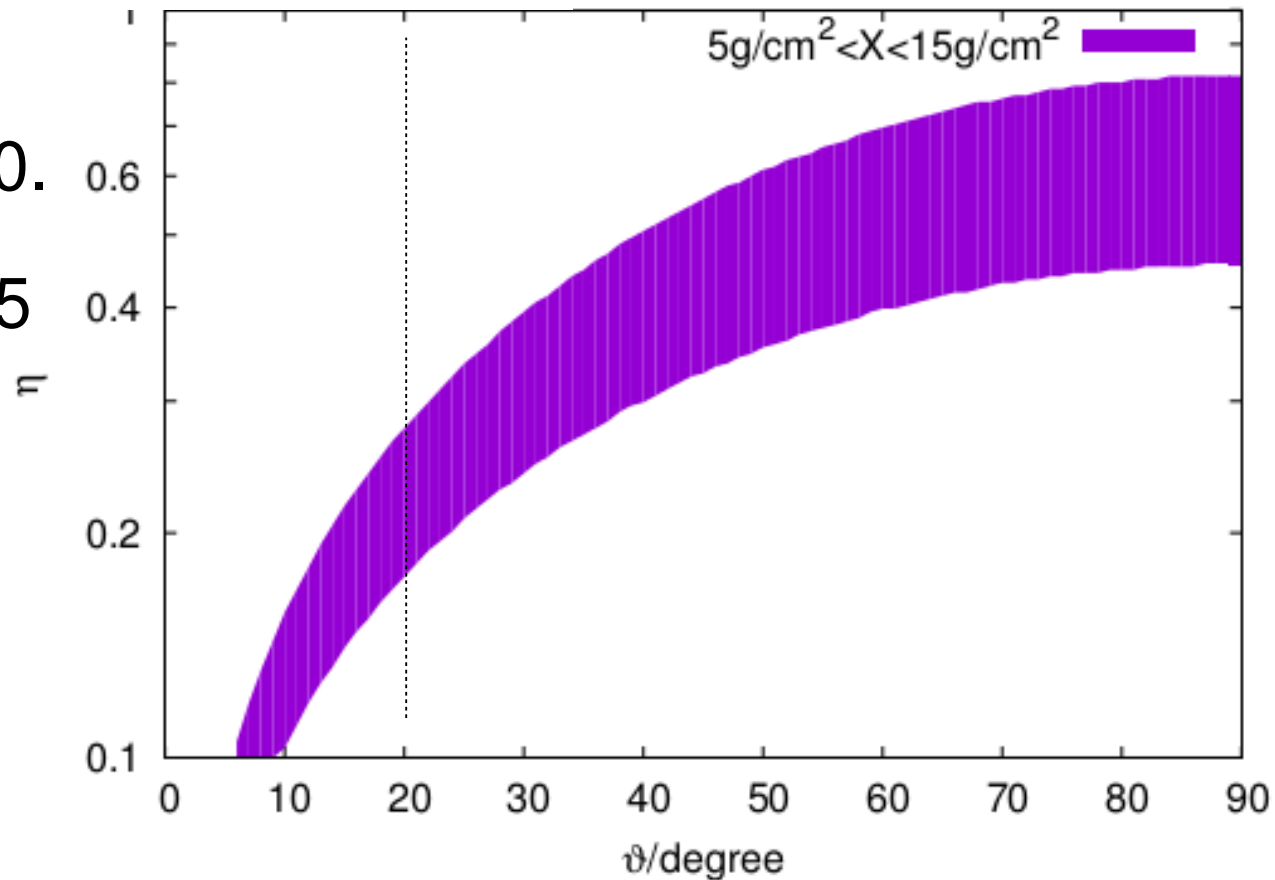
“X-field”
=> CRs go in the halo

$X(E)$ reproduced if TF
reduced by a factor $\approx 8-10$.

(1) Avg turb. level $\eta \approx 0.25$
along CR trajectories

(2) typically, $\Theta \approx 20^\circ$

=> Consistent picture



**Breakdown of the steady-state picture at low $E > \sim 1$ TeV?
Can a single 2–3 Myr source dominate the CR flux at 10 TeV?**

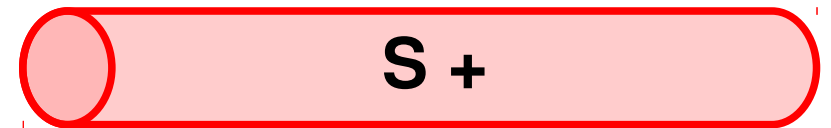
CR flux from a source at distance L and age t , after release :

$$10^{50} \text{ erg} \quad Q(E) = Q_0 (E/E_0)^{-\alpha} \quad \alpha \simeq 2.2$$

(1) At $2Dt \lesssim L^2$ flux suppressed.

(2) Later : $I(E) \simeq \frac{c}{4\pi} \frac{Q(E)}{V(t)}$

$$V(t) = \pi^{3/2} D_{\perp} D_{\parallel}^{1/2} t^{3/2} \quad \text{where} \quad 2Dt \sim L^2$$



(3) Even later : Escape from the Galaxy.

Case of isotropic diffusion:

$$D_{\text{iso}}(E_*) \sim 5 \times 10^{29} \text{ cm}^2/\text{s} \quad \text{satisfying the B/C constraints (H} \sim 5 \text{ kpc)}$$
$$E_* = 10 \text{ TeV}$$

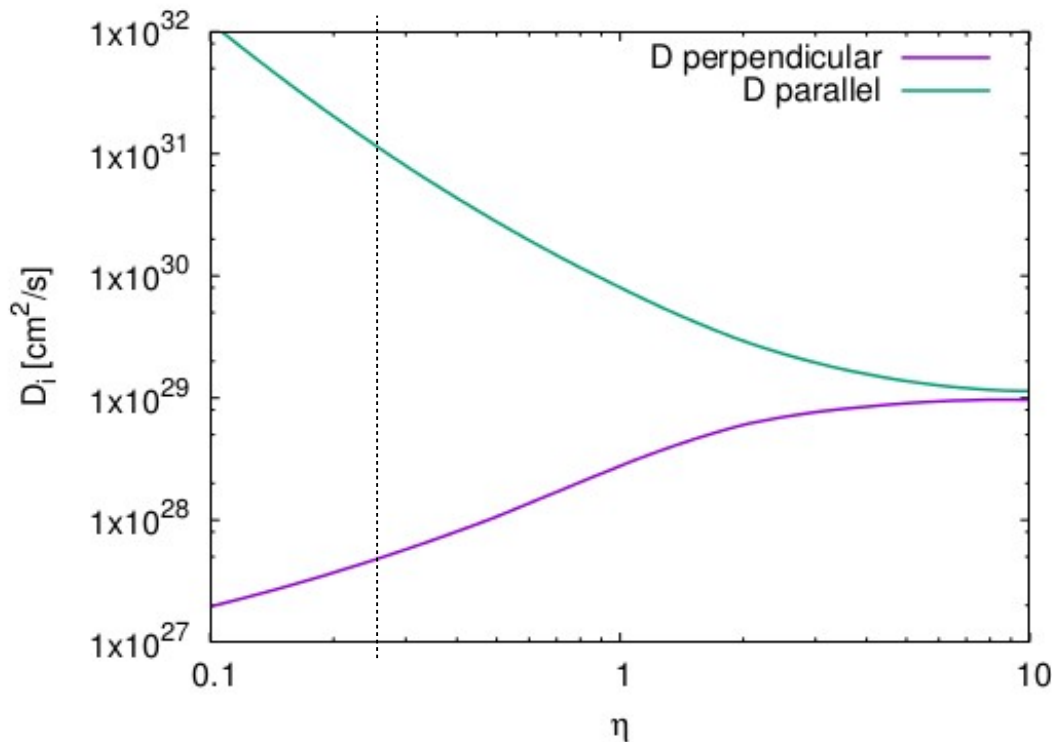
Size of the diffusion front at $t = 2 \text{ Myr}$: $L(t) = \sqrt{2Dt} \simeq 2.5 \text{ kpc}$

$$E_*^{2.8} I(E_*) \simeq 200 \text{ GeV}^{1.8} \text{ sr}^{-1} \text{ s}^{-1} \text{ m}^{-2}$$

→ Only 1/100 of observed CR intensity at E_*

=> NO! Large number of sources contribute to the CR flux.

Anisotropic diffusion (with JF GMF model):



$\eta = 0.25$ and $D_{\text{iso}} \simeq 2 \times 10^{30} \text{ cm}^2/\text{s}$
valid at $E = 10^{15} \text{ eV}$

$$\Rightarrow D_{\parallel} \simeq 5D_{\text{iso}}$$

$$\text{and } D_{\perp} \simeq D_{\text{iso}}/500$$

the volume $V(t) = \pi^{3/2} D_{\perp} D_{\parallel}^{1/2} t^{3/2}$ is reduced by $500/\sqrt{5} \simeq 200$

\Rightarrow A single source can contribute a fraction of order $O(1)$ to the total CR intensity at such E .

Part II: Conclusions and perspectives

- Isotropic Kolmogorov (Kraichnan) turbulence: Overproduce secondary nuclei (e.g. B) for any reasonable L_c , B_{rms}
- Strongly **anisotropic propagation** of CRs in the Milky Way: **Anisotropic diffusion** (+ Anisotropic turbulence ?)
- - Geometry of **regular Galactic magnetic field** important
 - Nb sources contributing to CR flux reduced by ~ 100
 - **Single source** may start to dominate at $>\sim$ TeV energies